



# Multiplication and Division



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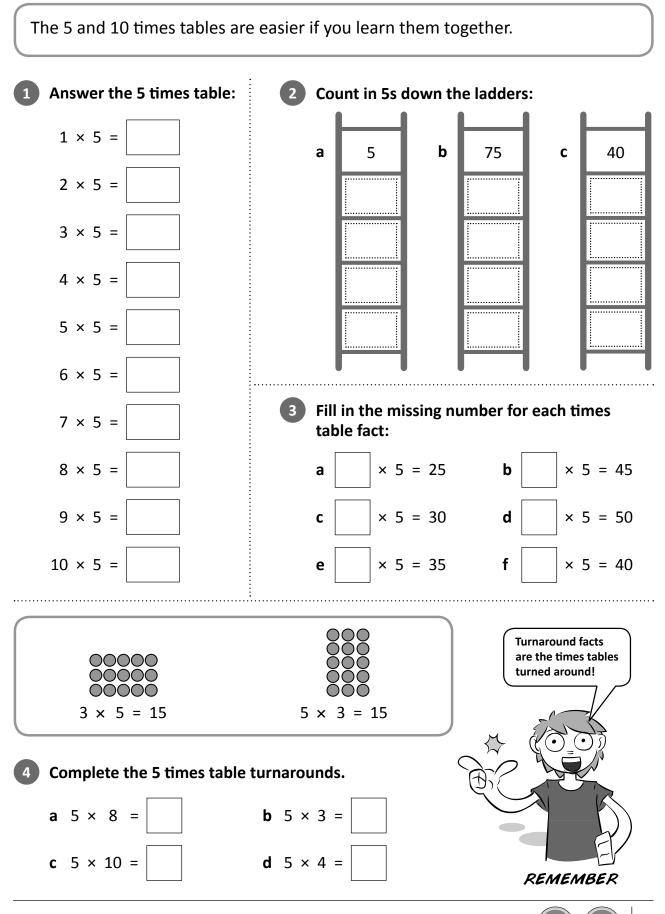
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## Multiplication facts – 5 and 10 times tables

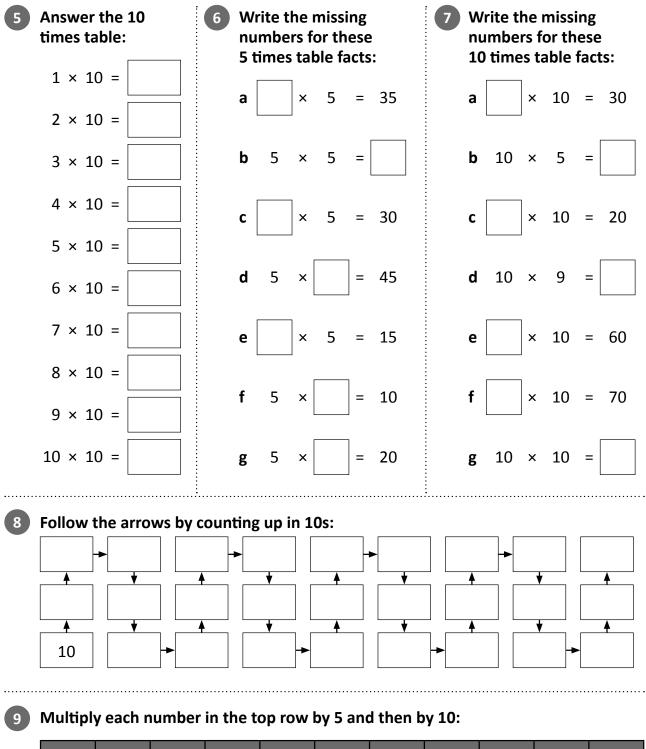


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#### Multiplication facts – 5 and 10 times tables

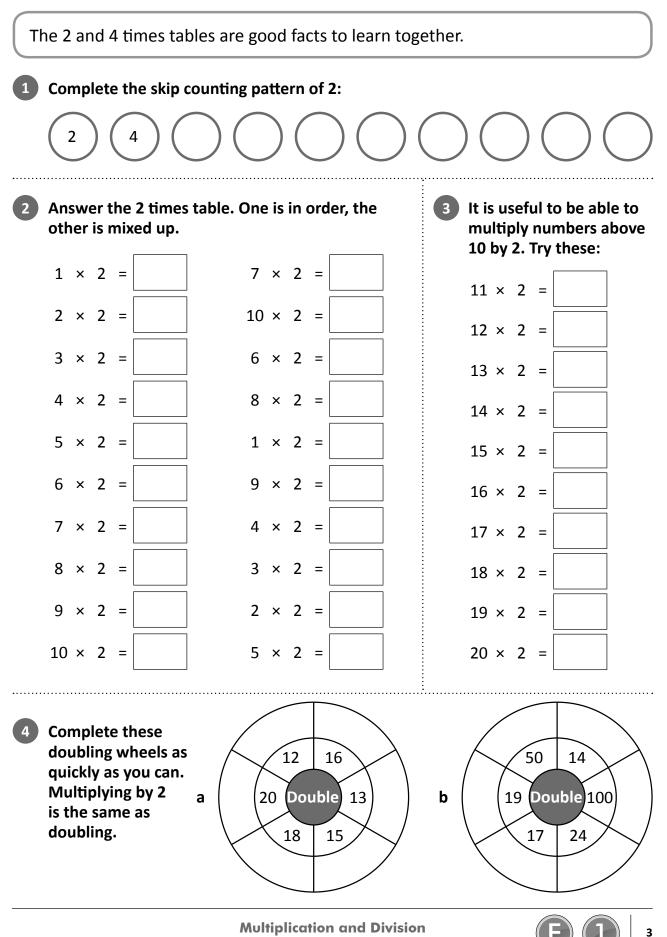


×	2	1	4	5	9	6	8	7	10	3
5										
10										

What do you notice?



# Multiplication facts – 2 and 4 times tables

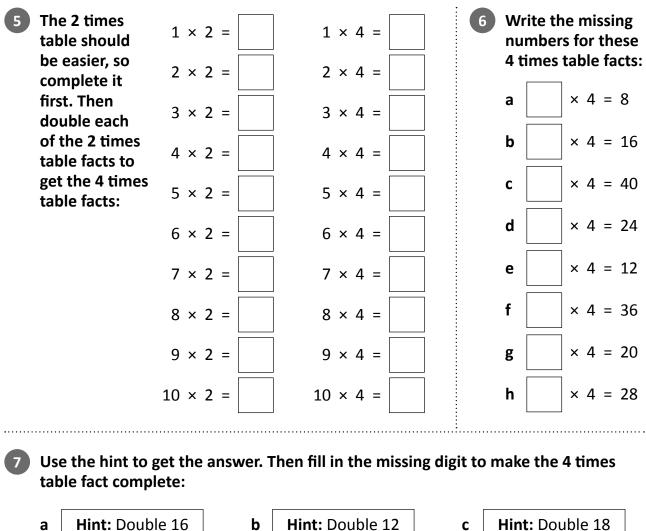


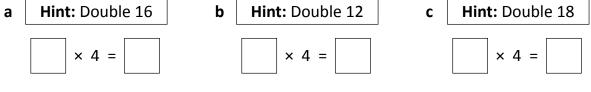
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#### Multiplication facts – 2 and 4 times tables

Now for the 4 times table. The 4 times table is just double the 2 times table. This is handy to remember if you forget a 4 times table fact.



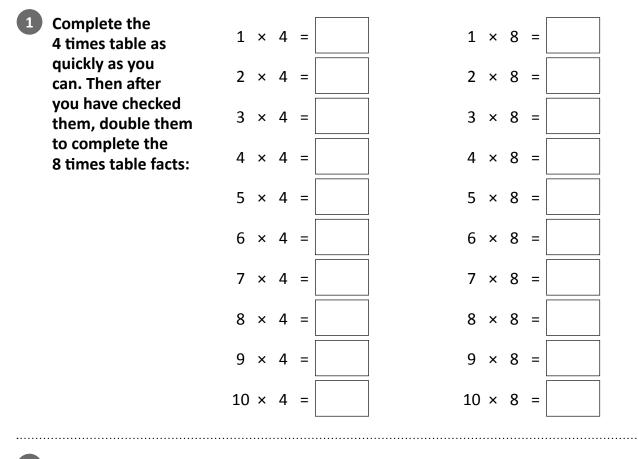


8 Look at the numbers in the grid and circle 3 numbers that would make a multiplication fact. Look for × 2 and × 4 facts. They are either left to right or top to bottom. The first one has been done for you. There are 10 to find.

4	3	12	4	8	32
4	1	3	2	7	1
16	5	3	8	2	9
3	4	6	24	14	4
2	8	16	7	9	36
9	2	18	10	2	20



Here is the 8 times table. You can double the 4 times table to get the 8 times table.



Use double, double and double again for these problems:

**a**  $6 \times 8 =$  **b**  $4 \times 8 =$  **c**  $9 \times 8 =$ 

2

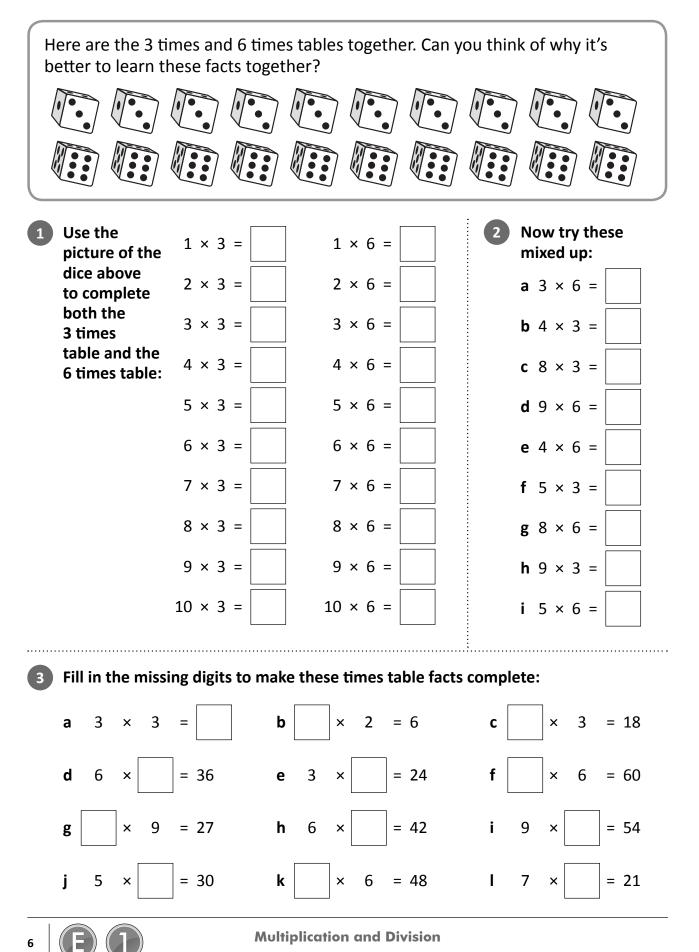
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- If you get stuck on the 8s, think double, double and double again. For example, 3 × 8 Think: double 3 is 6 double 6 is 12 double 12 is 24

On Mia's calculator, the 8 key is broken. Show her the steps she could follow to find the answer to 16 × 8. Use a calculator to test the steps.



#### Multiplication facts – 3 and 6 times tables

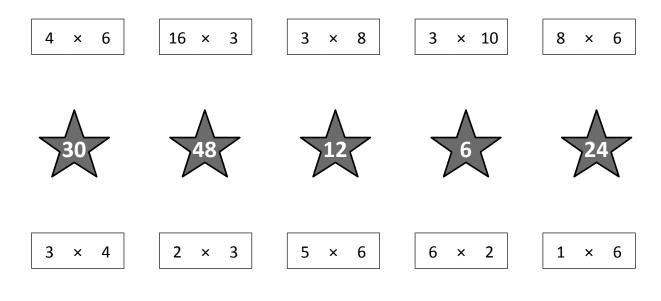


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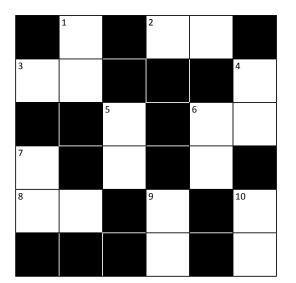
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## Multiplication facts – 3 and 6 times tables

Match the answers to the questions. Each answer has two matching questions.



#### Complete the cross number puzzle:



Across	Down
2. 9 × 3	1. 8 × 6
3. 3 × 6	4. 10 × 6
6.5×6	5. 9 × 6
8. 7 × 6	6. 6 × 6
	7.4×6
	9.6×3
	10. 7 × 3

.....

What number am I? I am in the 3 times table, 4 times table and 6 times table. I'm not 12.

l am

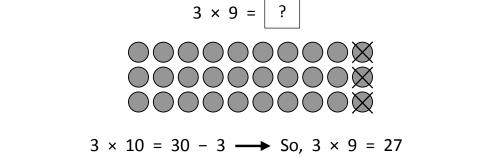
6

4

5



If you get stuck on a 9 times table fact, you can use the 10 times table facts and then build down.



Think of the × 10 facts and build down to get the × 9 facts. The first one is done for you.

× 10 table	Build down by	× 9 table
1 × 10 = 10	1	$1 \times 9 = 9$
2 × 10 = 20		
3 × 10 = 30		
4 × 10 = 40		
5 × 10 = 50		
6 × 10 = 60		
7 × 10 = 70		
8 × 10 = 80		
9 × 10 = 90		
10 × 10 = 100		

#### 2 Complete the × 9:

×	2	6	4	8	3	9	10	5	7
9									



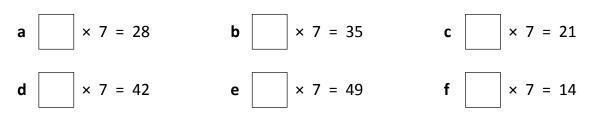
If you get stuck on a 7 times table fact, remember the 8 times table fact and build down.

× 8 table	Build down by	× 7 table
1 × 8 = 8	1	1 × 7 =
2 × 8 = 16	2	2 × 7 =
3 × 8 = 24	3	3 × 7 =
4 × 8 = 32		4 × 7 =
5 × 8 = 40		5 × 7 =
6 × 8 = 48		6 × 7 =
7 × 8 = 56		7 × 7 =
8 × 8 = 64		8 × 7 =
9 × 8 = 72		9 × 7 =
10 × 8 = 80		10 × 7 =

#### Think of the × 8 table fact and build down to get the × 7 table fact.



**2** Add the missing numbers to each fact:



**3** Use the × 8 to complete the × 7:

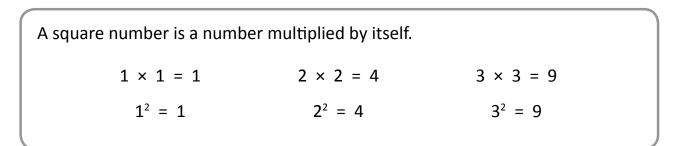
×	4	2	6	1	9	5	3	7	8
8									
7									



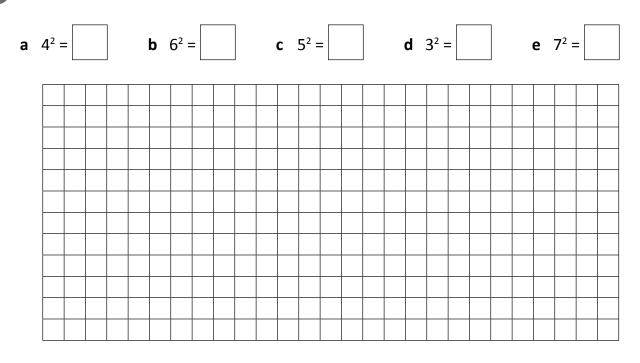
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#### Using known facts – square numbers



Show these square numbers on the grid and write what they are equal to:



2 Shade the square numbers on this multiplication grid:

×	2	3	4	5	6	7	8	9	10
2	4	6	8	10	12	14	16	18	20
3	6	9	12	15	18	21	24	27	30
4	8	12	16	20	24	28	32	36	40
5	10	15	20	25	30	35	40	45	50
6	12	18	24	30	36	42	48	54	60
7	14	21	28	35	42	49	56	63	70
8	16	24	32	40	48	56	64	72	80
9	18	27	36	45	54	63	72	81	90
10	20	30	40	50	60	70	80	90	100

#### **Multiplication and Division**

### Using known facts – factors and multiples

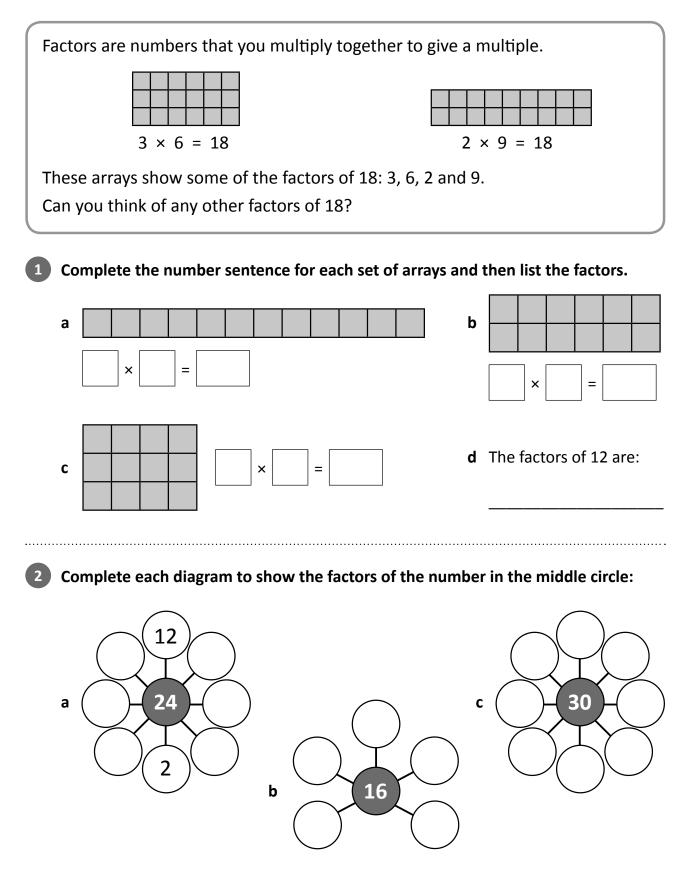
When 2 numbers are multipled together, the answer is called a multiple. The first 3 multiples of 2 are 2, 4, 6.

 $1 \times 2 = 2$   $2 \times 2 = 4$   $3 \times 2 = 6$ 

5, 10, 15, 20, 25, 30, 35, 40, 45, 50 are the first 10 multiples of 5.

List the first ten multiples of each number: 6 **a** 6 2 **b** 2 **c** 10 **d** 3 **e** 4 Write these numbers in the correct spots on the Venn diagram: The space in the diagram where the circles overlap is where 8 4 9 6 12 3 you put numbers that are both multiples of 2 and 3. Multiples **Multiples** of 2 of 3 ..... ...... THINK Can you think of any other numbers up to 60 that could go into the overlapping space in the Venn diagram above?

# Using known facts – factors and multiples





## Mental multiplication strategies – multiplying by 10 and 100

When we multiply any number by 10, a zero goes in the ones column and the digits all move one space along to the left.

When we multiply any number by 100, a zero goes in both the ones and the tens columns and all the digits move two spaces along to the left.

Thousands	Hundreds	Tens	Ones	
		4	5	
	4	5	0	× 10
4	5	0	0	× 100

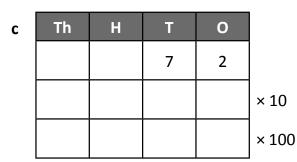
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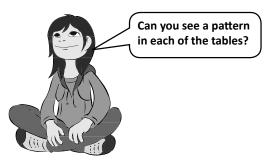
2

Use the place value tables to multiply these numbers by 10 and 100:

а	Th	Н	Т	0	-
			1	5	
					× 10
					× 100

b	Th	н	Т	0	
			4	8	
					× 10
					× 100





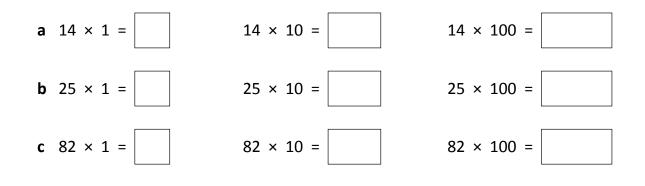
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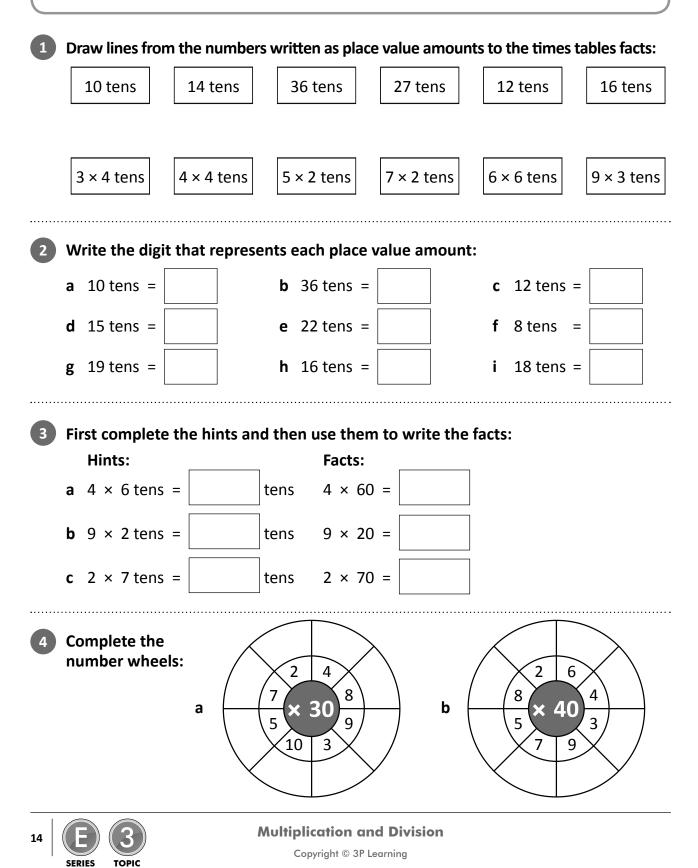
Use patterns to solve these:



**Multiplication and Division** 

How do you multiply by other multiples of 10? Let's look at 8  $\times$  20. We can use known times tables facts and write this as place value amounts:

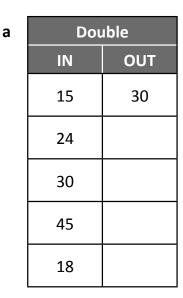
 $8 \times 2$  tens = 16 tens So,  $8 \times 20 = 160$ 

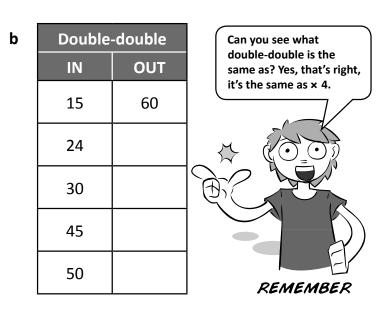


# Mental multiplication strategies – doubling strategy

There are many double facts that you should know.This includes numbers outside the times tables we have been working on.Here are 2 double facts that are handy to know:double 15 is 30 double 50 is 100 Can you think of more?

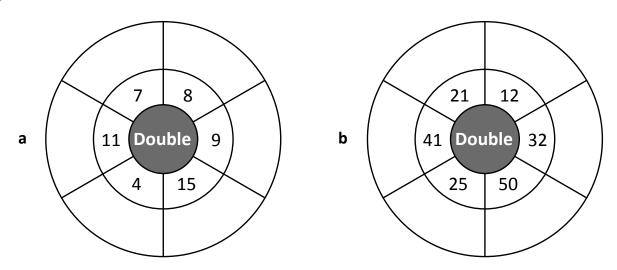
Complete these function machines:





2

**Complete these doubling wheels:** 





#### Mental multiplication strategies – doubling strategy

We also use doubling when we multiply by 4 and by 8. To multiply a number by 4, To multiply a number by 8, double it 3 times. double it twice.  $10 \times 4 = 40$  $11 \times 8 = 88$ Double 10 once 20 Double 11 once 22 Double 10 twice 40 Double 11 twice 44 Double 11 three times 88

Keep doubling to get the × 4 and × 8 facts. Here are some tables to help you. The first one has been done for you.

1

16

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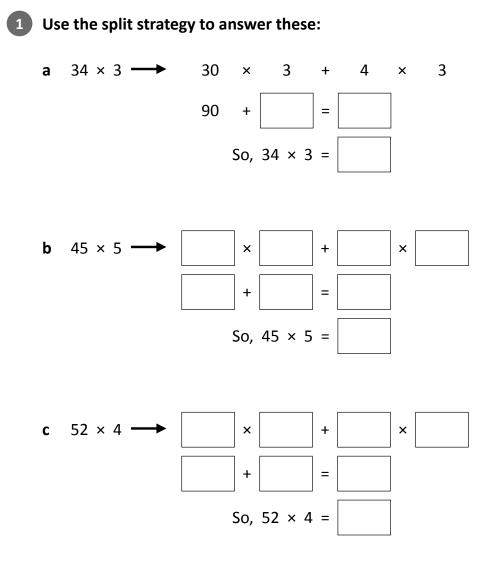
а	12 × 4 = 48		b	15 × 4 =		
	Double 12 once	24		Double 15 once		
	Double 12 twice	48	]	Double 15 twice		
С	18 × 4 =		d	22 × 4 =		
	Double 18 once			Double 22 once		
	Double 18 twice			Double 22 twice		
е	16 × 8 =		f	35 × 8 =		
	Double 16 once			Double 35 once		
	Double 16 twice			Double 35 twice		
	Double 16 three times			Double 35 three times		
			g	× 8 =		
	In this last table choose a 2-digi	t		Double once		
number to multiply by 8 and double it three times.				Double twice		
ſ				Double three times		
E	(F) (3) Multiplication and Division					

#### Mental multiplication strategies – split strategy

The split strategy is when we multiply numbers in 2 pairs and then add the parts. Let's use the split strategy for  $26 \times 4$ .

- Split 26 into 20 and 6.
- Multiply each part.
- Add the answers together.

```
26 \times 4 \longrightarrow 20 \times 4 + 6 \times 4
80 + 24 = 104
So, 26 \times 4 = 104
```





#### Mental multiplication strategies – compensation

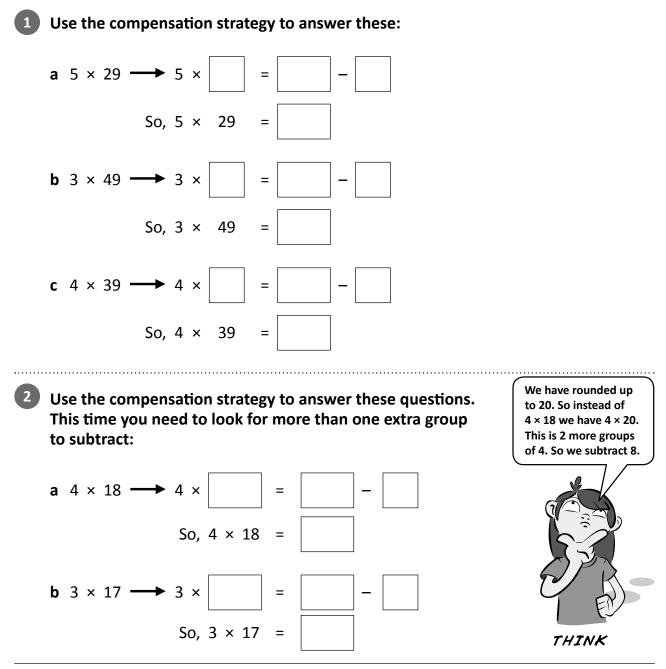
Use the compensation strategy to make it easier to multiply 2-digit numbers that are close to a ten.

Look at  $4 \times 19$ .

19 is close to 20, so we can multiply by the next multiple of ten which is 20. Then we build down because we have an extra group of 4.

 $4 \times 19 \longrightarrow 4 \times 20 = 80 - 4$ 

So, 19 × 4 = 76





#### Mental multiplication strategies – choose a strategy

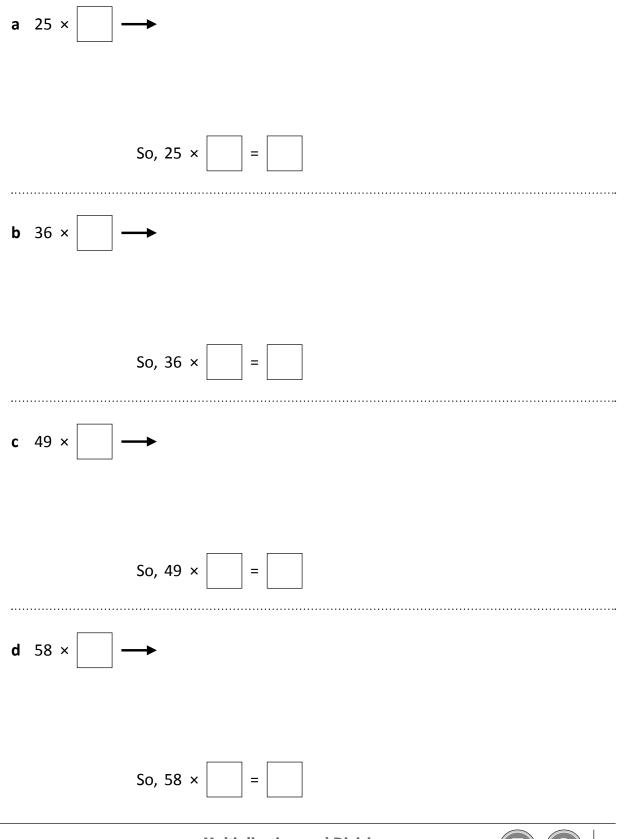
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Roll a die to get the missing number, then use either the split or compensation strategy to get the answer. You can place the numbers rolled on the die in any question.



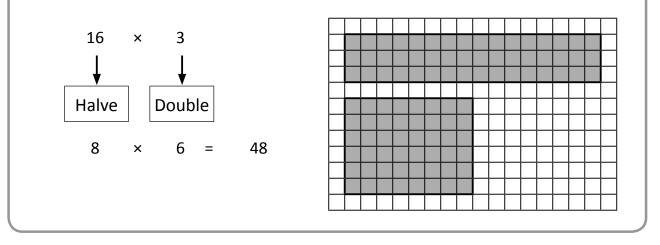
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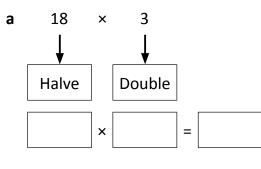


#### Mental multiplication strategies – doubling and halving

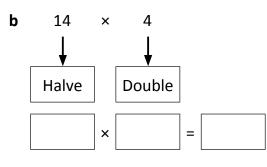
We can change the factors of a multiplication question to make it easier. Look at  $16 \times 3$ . If we halve the larger factor and double the smaller factor, we make an array on the grid that is the same size. Both arrays have the same amount of squares. Count the squares, are they equal to  $8 \times 6$ ?

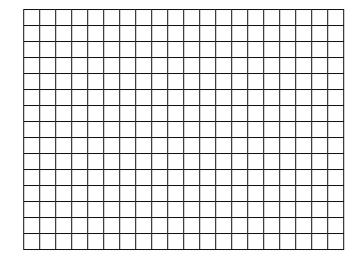


Make these problems easier by using doubling and halving. Shade an array for each:



,	 									
$\square$										Γ
$\square$										

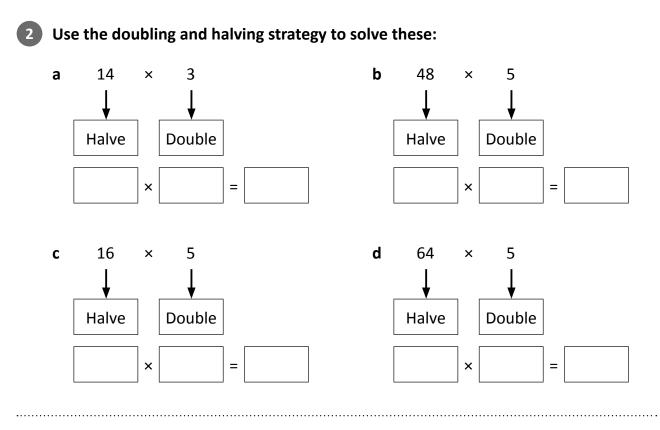




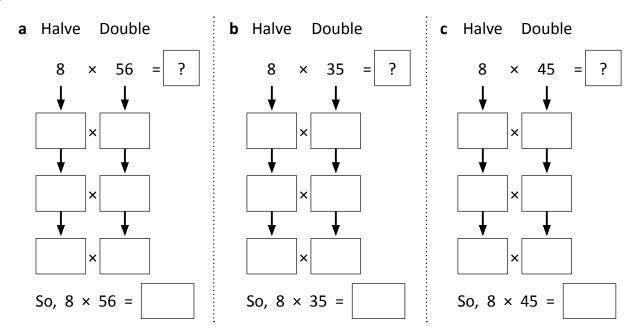


#### **Multiplication and Division**

#### Mental multiplication strategies – doubling and halving



Follow this doubling and halving trail through to the bottom:

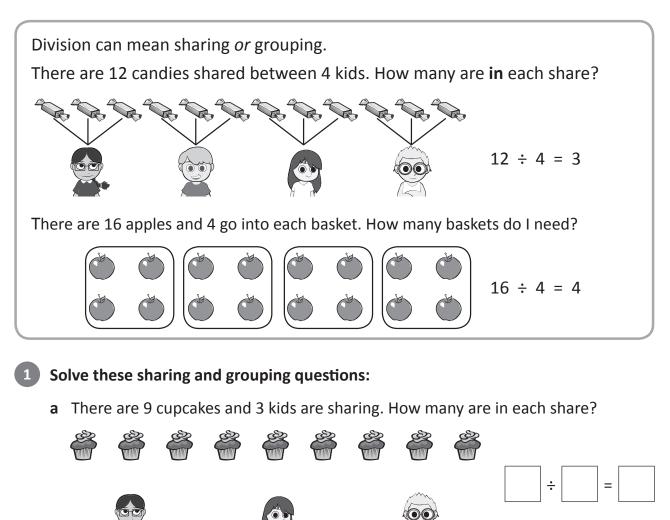


**d** What do you notice?

3



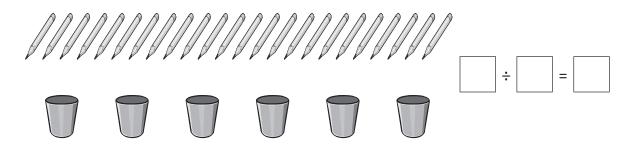
# Division – division is sharing and grouping



**b** 10 candies are shared between a group of kids so they each get 2. How many kids are sharing?



**c** There are 24 pencils and 6 pencil pots. How many pencils go into each pencil pot?





#### **Multiplication and Division**

# Division – division is sharing and grouping

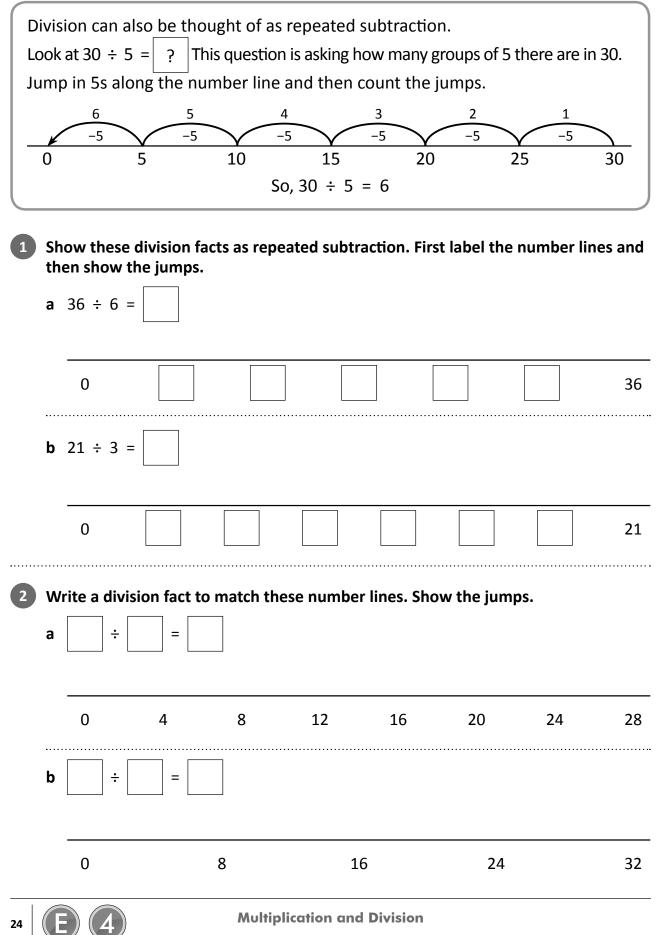
2 Draw pictures to show these division questions. Then write the division fact and decide whether it is a sharing or a grouping question. If you need to find out how many items there are in each share, it's a sharing question. If you need to find out the number of equal shares, it's a grouping question.



<b>a</b> Divide 16 candies between 4 girls. How many does each girl get?						
	÷ =					
	sharing / grouping					
b From a packet of 24 pencils, each person will get 6 sharing the pencils?	. How many people are					
	÷ =					
	sharing / grouping					
c 48 eggs are laid by 6 hens. If they all laid the same each hen lay?	amount, how many did					
	÷ =					
	sharing / grouping					



## Division – division is repeated subtraction



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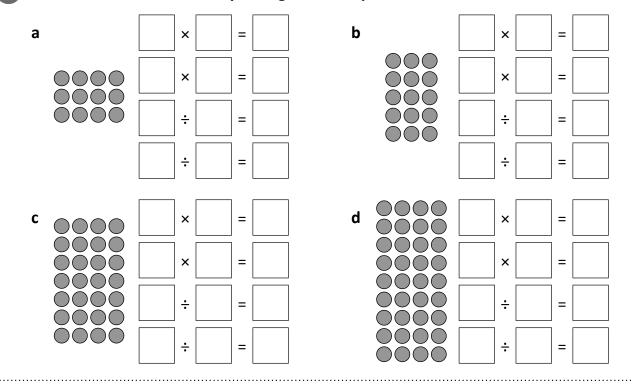
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# Division – linking multiplication and division facts

Knowing multiplication facts will help with division facts. This is because they are opposites. Look at how we can describe this array:

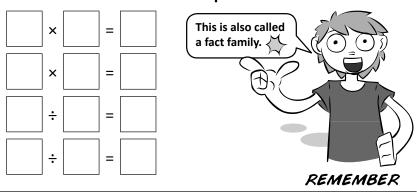
$\bigcirc \bigcirc $	6 × 4 = 24	6 groups of 4 is 24.
$\bigcirc \bigcirc $		
$\bigcirc \bigcirc $	4 × 6 = 24	4 groups of 6 is 24.
$\bigcirc \bigcirc $	24 ÷ 4 = 6	24 divided into 4 shares is 6.
$\bigcirc \bigcirc $		
$\bigcirc \bigcirc $	$24 \div 6 = 4$	24 divided into 6 shares is 4.

Describe each of these arrays using two multiplication and two division facts:



Draw an array of 6 rows of 3 then describe it with multiplication and division facts.

2



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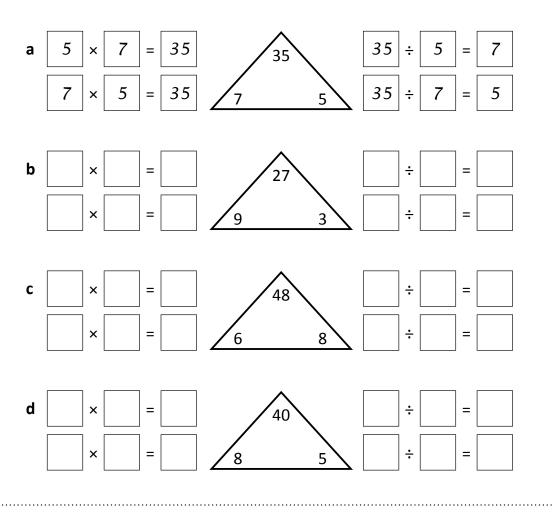
#### **Multiplication and Division**

#### Division – linking multiplication and division facts



4

3 Write a fact family for each set of numbers in the triangle. The first one has been done for you.

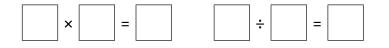


For these problems, think of a multiplication fact to help write the division fact:

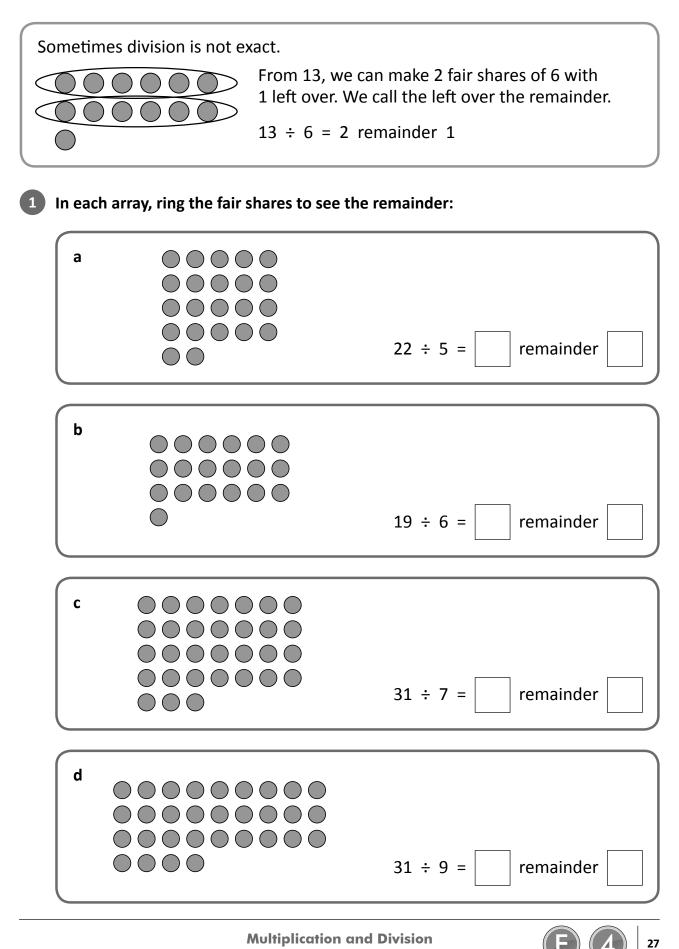
a \$25 is shared between 5 people. How much does each person get?



**b** 45 people get into 9 cars. How many people are in each car?



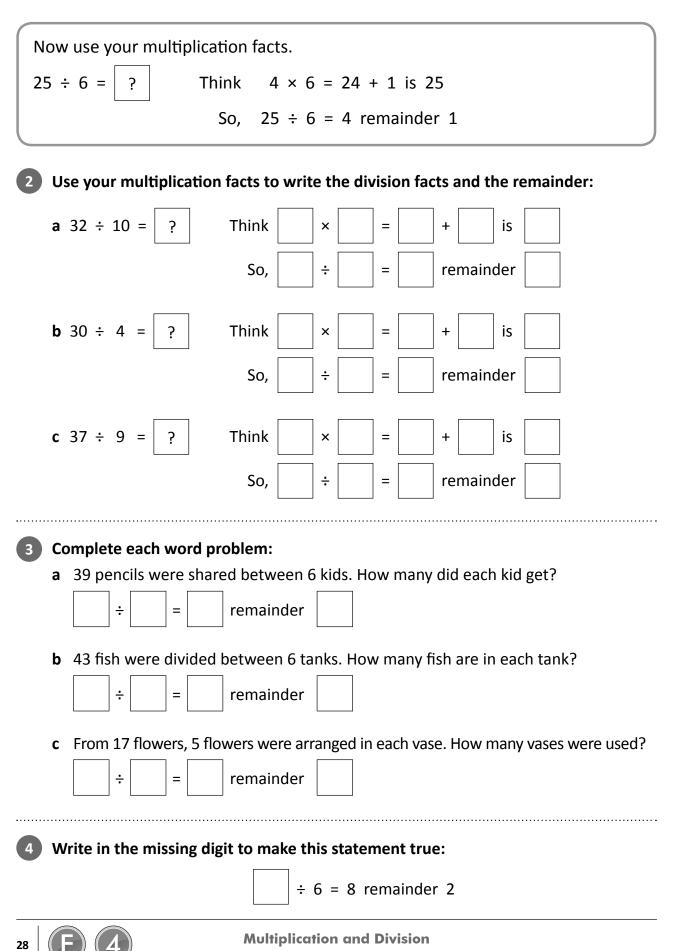




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#### Division – remainders



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# Mental division strategies – dividing by 10 and 100

When we divide any					_
number by 10, we move the number one place	Thousands	Hundreds	Tens	Ones	
value space to the right.	6	7	0	0	
When we divide any number by 100, we move		6	7	0	) ÷ 10
the number two place			6	7	÷ 100
value spaces to the right.		· · · · ·			

Use the place value tables to divide these numbers by 10 and 100.

а	Th	н	Т	0	
	5	3	0	0	
					÷10
					÷100

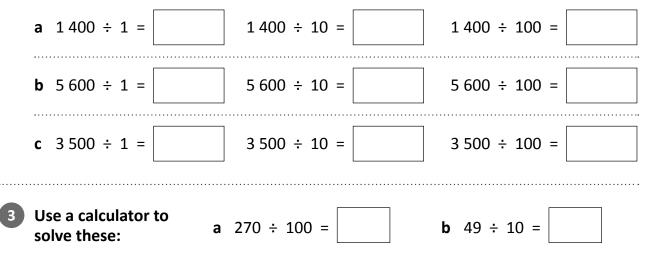
С	Th	н	Т	0	
	8	4	0	0	
					÷10
					÷100

b	Th	н	Т	0	
	4	1	0	0	
					÷10
					÷100

d	Th	н	Т	0	
	2	4	0	0	
					÷10
					÷100

#### Use patterns to solve these:

2



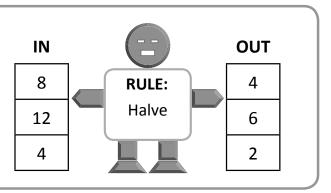
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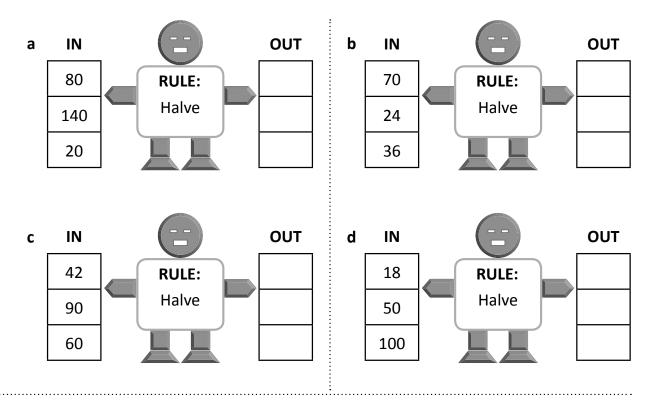
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### Mental division strategies – halving strategy

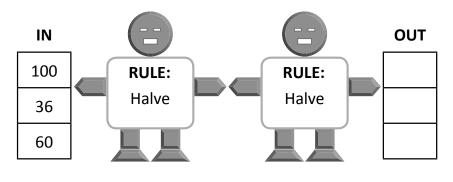
When you halve numbers you are dividing them by 2. In this function machine, numbers go IN, have the rule applied and come OUT again.



Complete the halving function machines. Halve the number going IN the machine and write the answer in the OUT column:



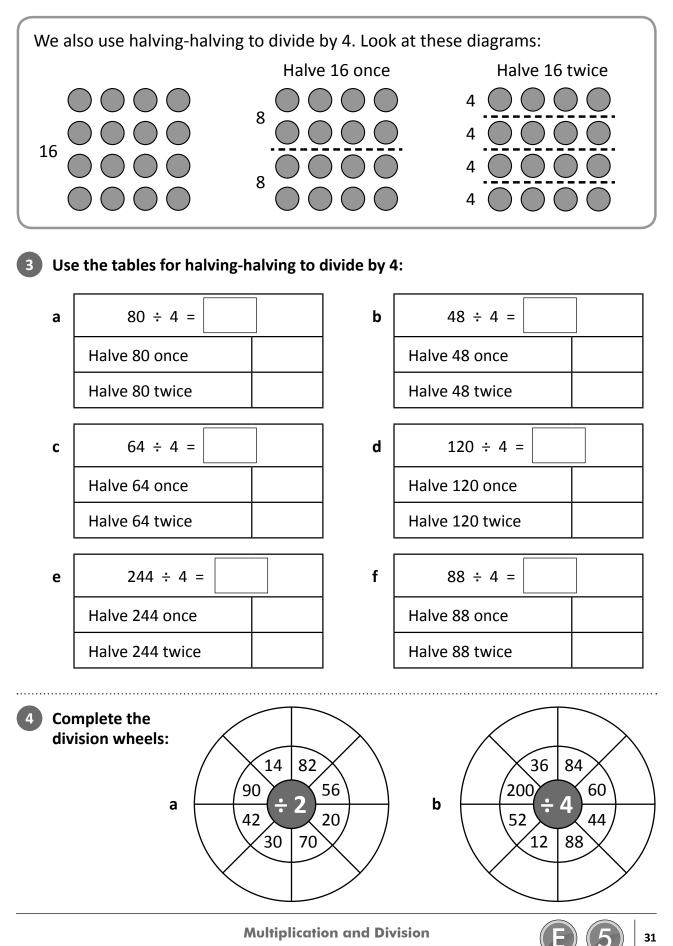
Below is a halving-halving function machine. The number goes IN and is halved and then halved again and comes OUT.





2

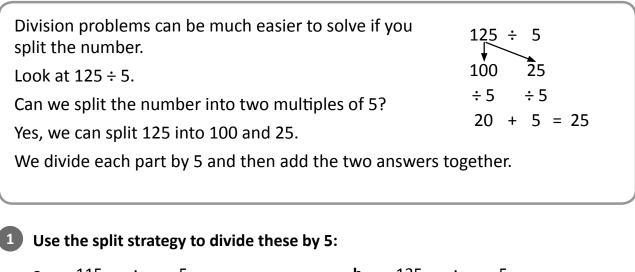
### Mental division strategies – halving strategy

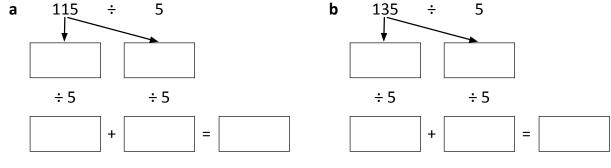


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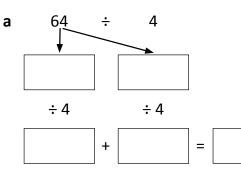
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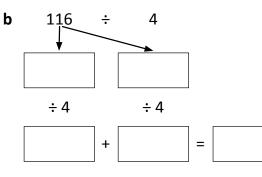
## Mental division strategies – split strategy



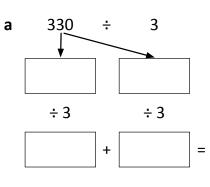


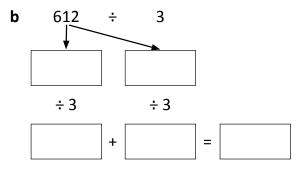
#### Use the split strategy to divide these by 4:





Use the split strategy to divide these by 3:







2

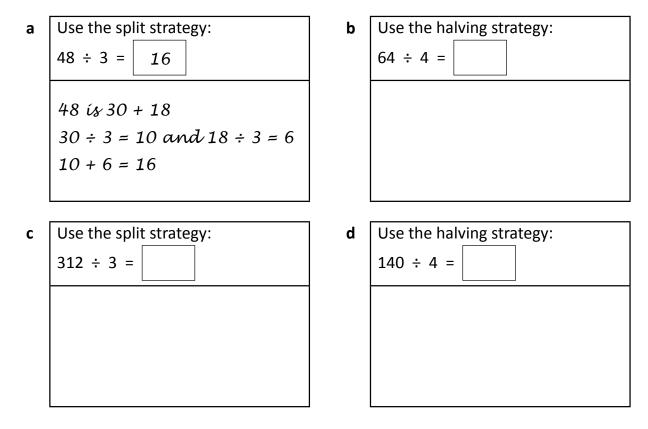
3

#### **Multiplication and Division**

Review your division strategies.

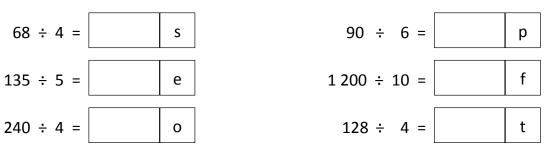


#### Use either the halving strategy or the split strategy to complete the tables. The first one has been done for you.



2 Solve this riddle by matching the letter to the answer. Use a mental division strategy for each problem.

#### What is it that the more you take, the more you leave behind?



120	60	60	32	17	32	27	15	17



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## Written methods – contracted multiplication

	н	т	0
		<sup>1</sup> 5	4
×	•		3
	1	6	2

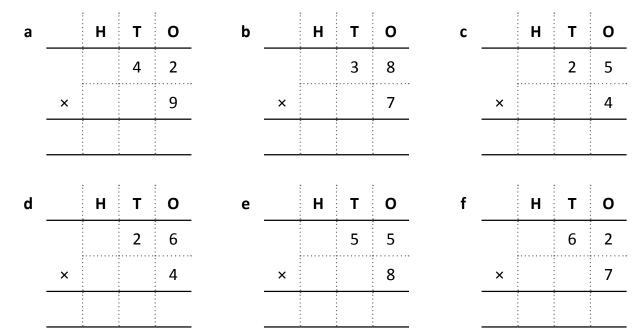
Start with the ones.  $4 \times 3 = 12$  ones.

Rename this as 1 ten and 2 ones. Put the 2 in the ones column and regroup the 1 to the tens column.

 $3 \times 5$  plus the regrouped 1 is 16 tens.

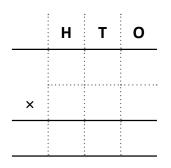
Rename this as 1 hundred and 6 tens.



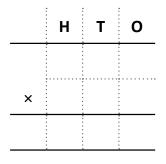


### Use contracted multiplication to solve these word problems:

**a** On a farm, 6 lambs were born every day over 25 days. How many lambs were born in total?



**b** For my school spirit day, I baked 9 trays of cupcakes. If there are 14 cupcakes on each tray, how many did I bake in total?

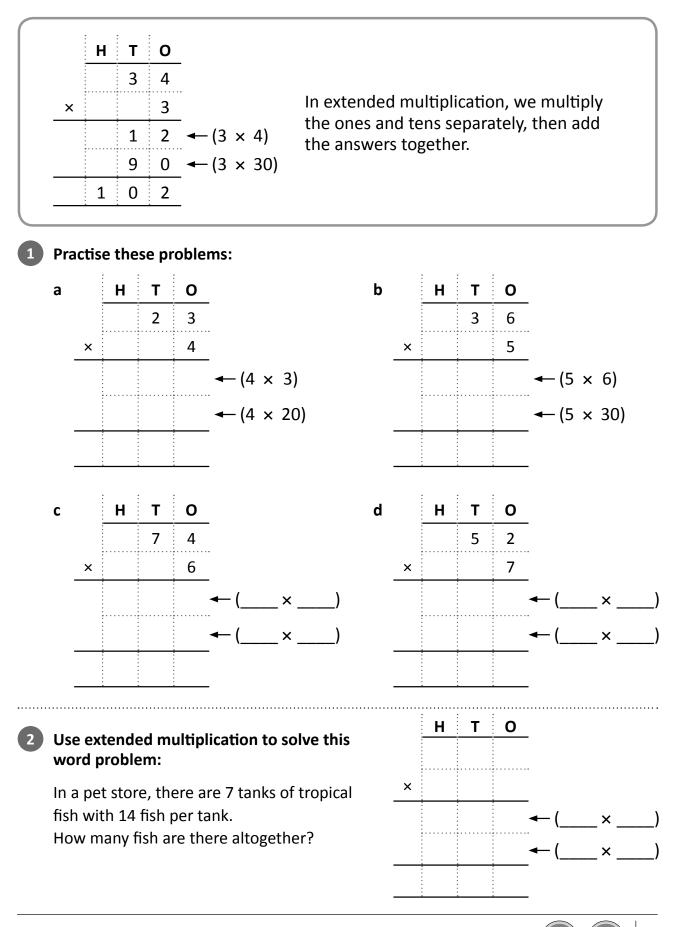




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2

## Written methods – extended multiplication



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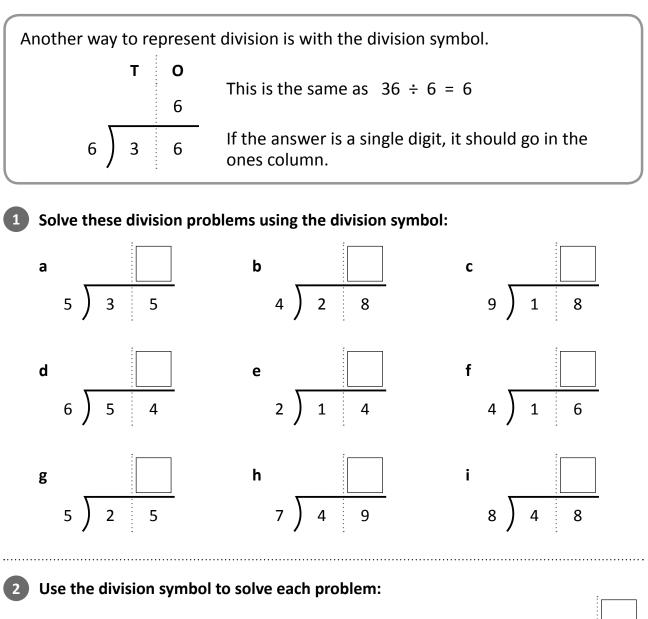
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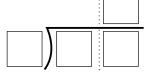
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35

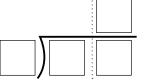
## Written methods – short division



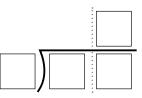
**a** 42 cupcakes were iced by 7 kids. If they each iced the same amount, how many did they ice each?



**b** How many pots were used if 6 seeds were planted in each pot from a packet of 54?

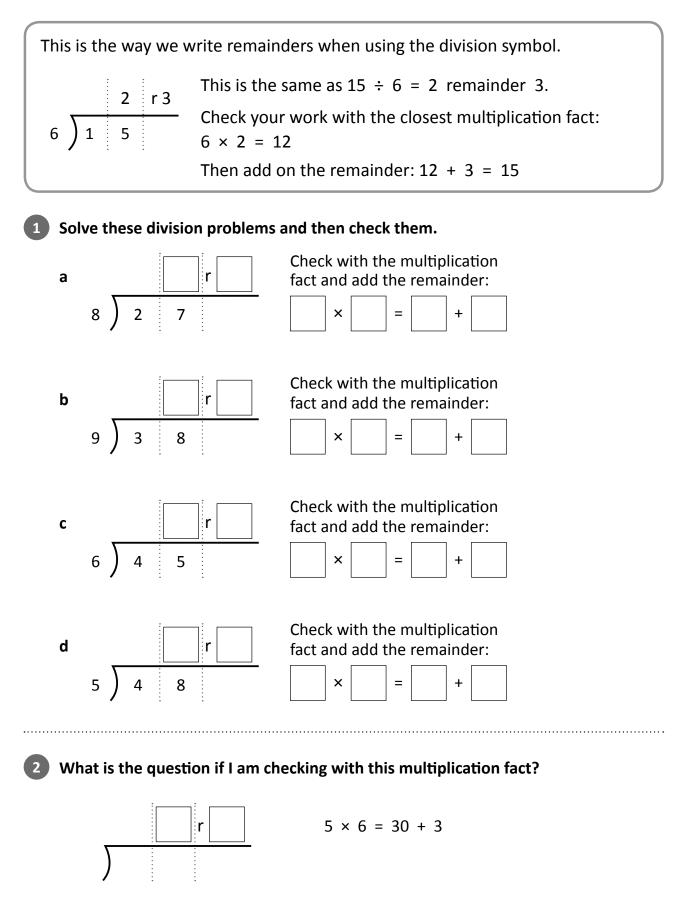


**c** I run the same distance each day. Over 9 days the total distance is 72 km. How far did I run each day?





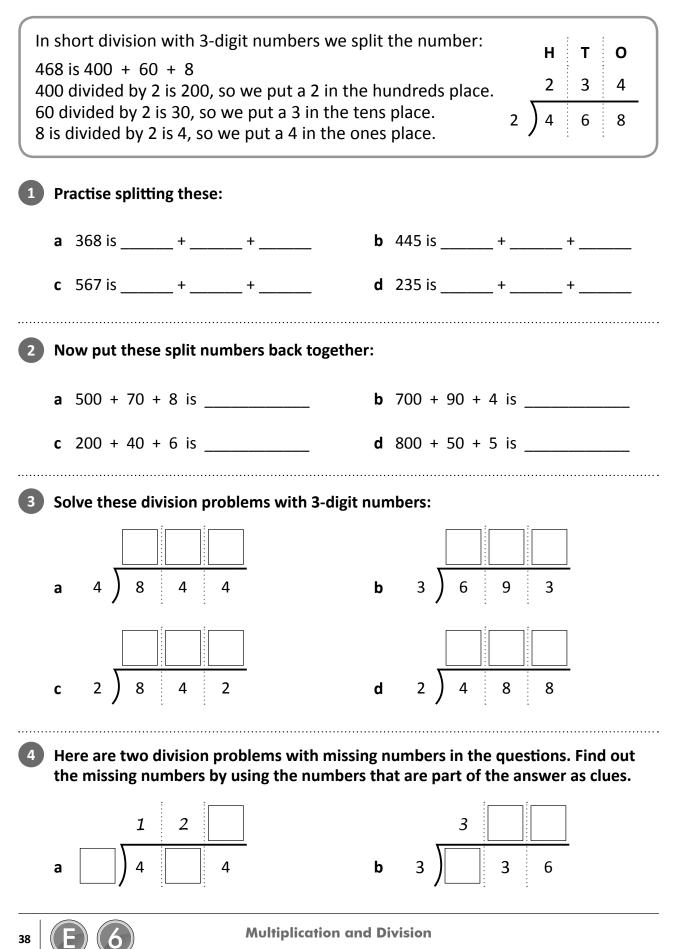
## Written methods – short division with remainders



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## Written methods – short division with 3-digit numbers

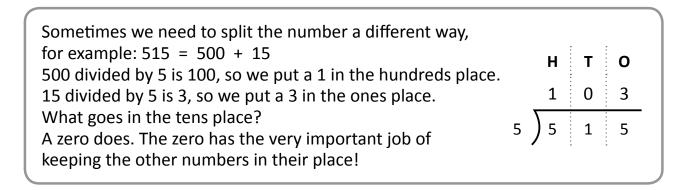


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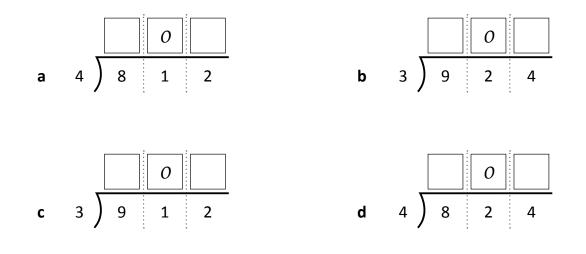
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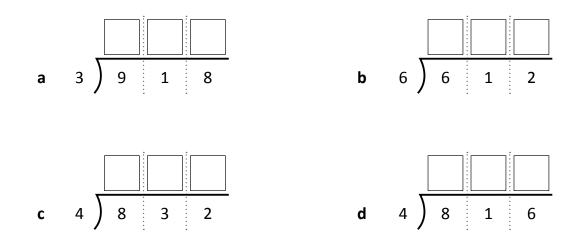
## Written methods – short division with 3-digit numbers

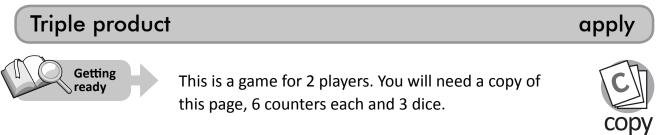


#### Practise these problems. We have put the zero in to remind you:



Practise these problems. This time, you need to remember the zero!









Player 1 rolls all 3 dice and chooses 2 of the numbers to multiply. If the player can see the answer in the grid, they claim this number by placing a counter over the number. Then Player 2 has a turn. The winner is the first to place all 6 counters on the grid.

20	15	12	2	8
6	12	6	16	6
36	20	18	8	10
12	10	6	12	4
10	12	15	24	25



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### Factor bingo

### apply



This is a game for three players. Each player needs a copy of this page. The caller needs a pile of the numbers from 1 to 9.





Each multiplication grid contains all the answers, while the factors are missing. Remember factors are the numbers that you multiply to get the answer.

The aim of the game is to be the first player to fill their grid with the factors. One hint is provided in each grid to start you off. Choose one person to be the caller and the other two play the round. The caller picks a number without looking and reads it out to the players. The players write it on the grids, if it fits as a factor. The first to fill in one of the grids completely is the winner.

,	<b>~</b>					 			
1	6	×				×	3		
•	•	6	42	24	18		12	20	28
2	7		63	36	27		18	30	42
			35	20	15		27	45	63
3	8		•	•	•				
		×				×			9
4	9		8	40	64		4	14	18
		3	3	15	24		2	7	9
5			9	45	72		12	42	54



### Doubling strategy to 20

### apply



This is a game for two players. You will need a copy of page 43, a die and a pencil to write down your scores. You may like to make extra copies of page 43 to play again later. COPY





The aim of this game is to score the highest number of points each time without going over 20. Roll the dice and choose which strategy you will use. From the Strategy column, circle 1 for double, 2 for double-double or 3 for double-double-double. For example, Player 2 has rolled a 5 and has chosen strategy 3 double-double. This makes a score of 40 but because it is over 20 it doesn't count. Look at the rest of the sample game to see how the game turned out.

Strategy 1	Strategy 2	Strategy 3
Double	Double Double	Double Double Double

#### Sample game

	Player 1			Player 2	
Die	Strategy	Score	Die	Strategy	Sco
6	1 2 3	12	5	1	4(
2	$ \begin{array}{c} 1\\ 2\\ \overline{3} \end{array} $	16	3	$\begin{array}{c}1\\\hline2\\3\end{array}$	1
4	$\begin{array}{c}1\\2\\3\end{array}$	16	1	1 2 3	8
6	1 2 3	24	4	$\begin{array}{c}1\\\hline2\\3\end{array}$	1(
3	$ \begin{array}{c} 1\\ (2)\\ 3 \end{array} $	12	2	1 2 3	10
	Total	56		Total	52



# Doubling strategy to 20

Strategy 1	Strategy 2	Strategy 3
Double	Double Double	Double Double Double

	Player 1		Player 2				
Die	Strategy	Score	Die	Strategy	Score		
	1			1			
	2			2			
	3			3			
	1			1			
	2			2			
	3			3			
	1			1			
	2			2			
	3			3			
	1			1			
	2			2			
	3			3			
	1			1			
	2			2			
	3			3			
	Total			Total			





apply

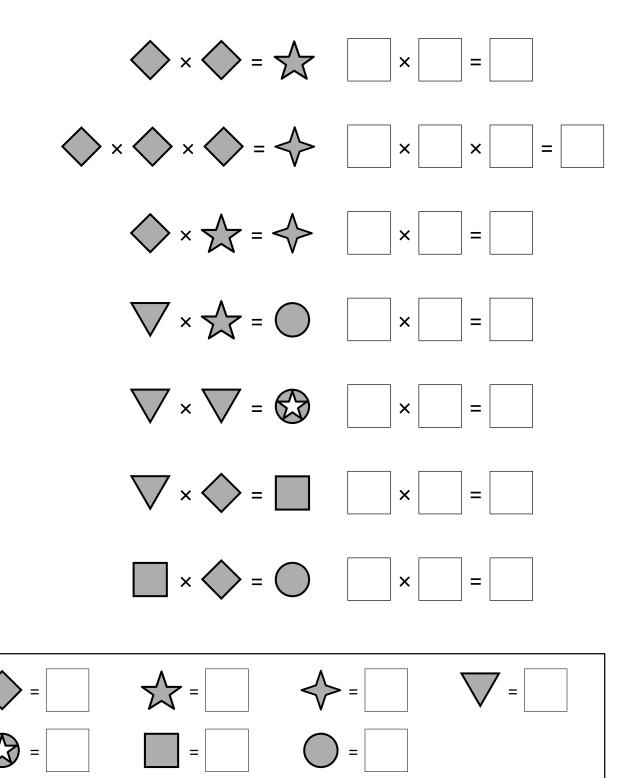
43

### **Symbols**



Can you work out the value of each symbol?

The values are 2, 3, 4, 6, 8, 9 and 12. Remember, the same symbol means that it's the same number.





#### **Multiplication and Division**

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