

name



# Fractions, Decimals and Percentages

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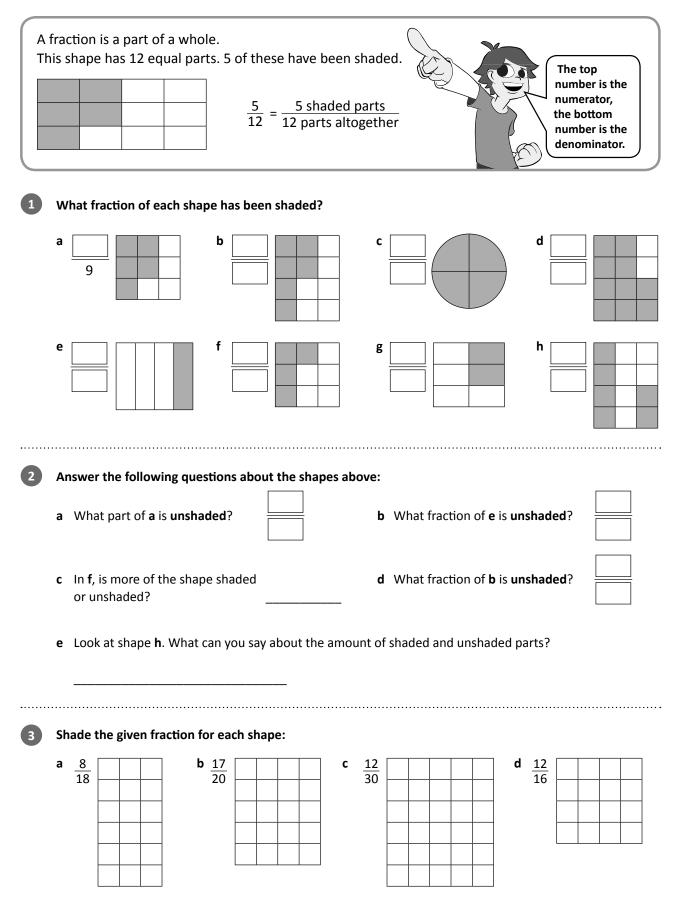
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## Series F – Fractions, Decimals and Percentages

#### Contents

Iopic 1 – Fract	ions (pp. 1–8)	Date completed
	fractions of shapes	/ /
	fractions of a collection	/ /
	comparing and ordering fractions	
	find the fraction – <i>solve</i>	
Topic 2 – Types	s of fractions (pp. 9–16)	
	equivalent fractions	
	equivalent fraction snap – <i>apply</i>	
	feeding time – <i>apply</i>	
Topic 3 – Fract	<ul> <li>ions, decimals and percentages (pp. 17–25)</li> <li>tenths</li> </ul>	
	tenths and hundredths	
	decimal place value	
	percentages	
	match 'n' snap – <i>apply</i>	
Topic 4 – Calcu	llating (pp. 26–34)	
	<ul> <li>adding and subtracting fractions with like denominators</li> </ul>	/ /
	<ul> <li>adding and subtracting fractions to and from a whole</li> </ul>	
	adding and subtracting fractions	
Series Authors:	adding decimal fractions	
Rachel Flenley	subtracting decimal fractions	
	• you cut, I choose – <i>solve</i>	

#### Fractions – fractions of shapes



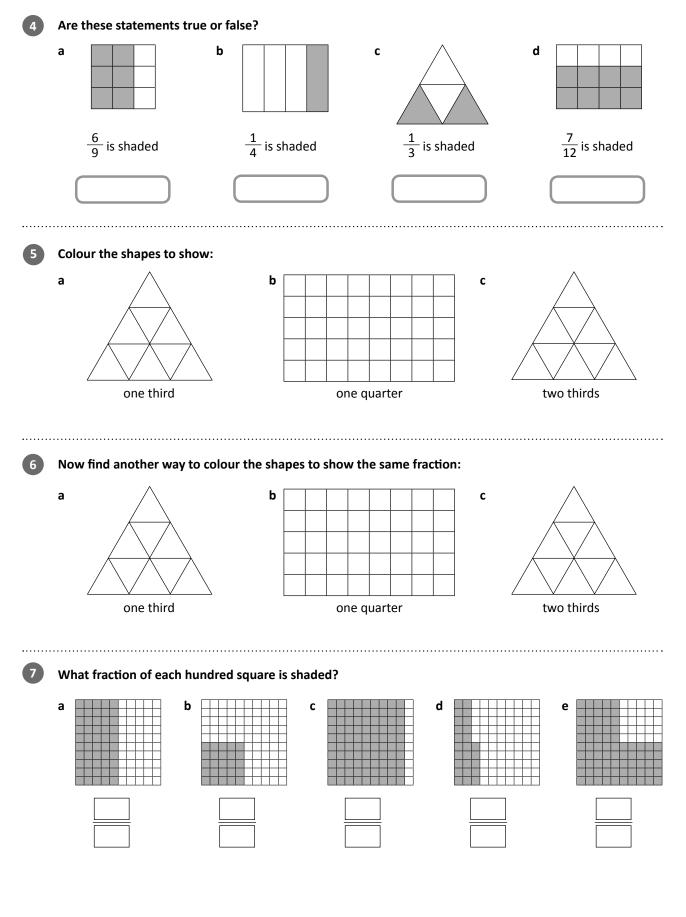
Fractions, Decimals and Percentages

1

SERIES

TOPIC

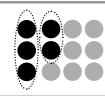
## Fractions – fractions of shapes





**Fractions, Decimals and Percentages** 

### Fractions – fractions of a collection

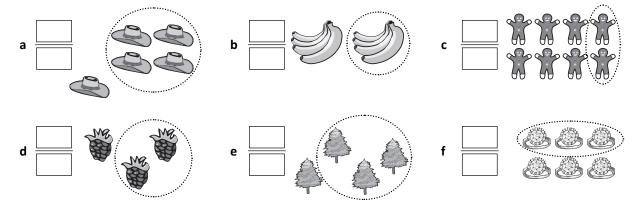


We can also have fractions of groups.

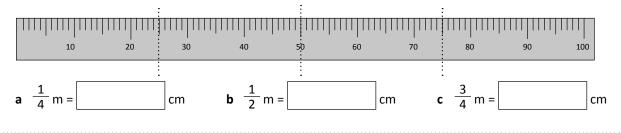
This is a group of 12 dots. 5 out of the 12 dots are circled.

We express this as  $\frac{5}{12}$ 

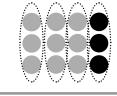
#### What fraction of each group has been circled?



Look at the metre ruler and work out how many centimetres are represented by the fraction:



Sometimes we are asked to find the fraction of an amount such as:



2

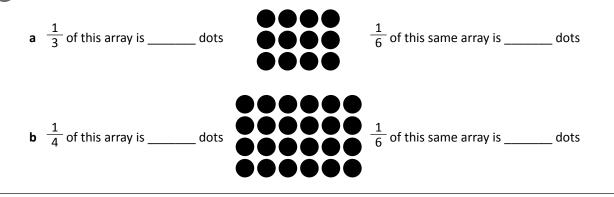
Find one quarter of this array.

There are 12 dots in the array.

First we divide the array into 4 equal parts.

There are 3 dots in each part or quarter so one quarter of 12 is 3.

Use the arrays to help find the given fractions of the groups:



Fractions, Decimals and Percentages

3

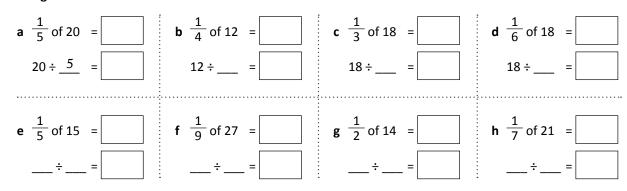
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#### Fractions – fractions of a collection

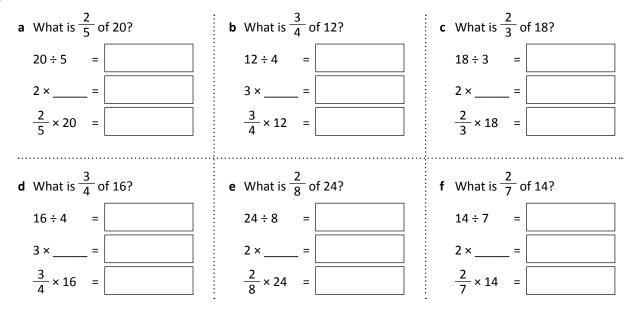
There is another way to find fractions of amounts:What is  $\frac{1}{4}$  of 20?20 divided into 4 groups is 5 in each group $20 \div 4 = 5$ 

Find the fractional amounts. You can use blocks or counters to help or solve the problems in your head using division:



Once we know how to find one part of a group, we can use this to find other amounts: To find  $\frac{2}{3}$  of 9, we first find  $\frac{1}{3}$  of 9  $\longrightarrow$  9 ÷ 3 = 3  $\frac{1}{3}$  of 9 = 3  $\frac{2}{3}$  of 9 is 2 times this  $\longrightarrow$  2 × 3 = 6  $\frac{2}{3}$  of 9 = 6

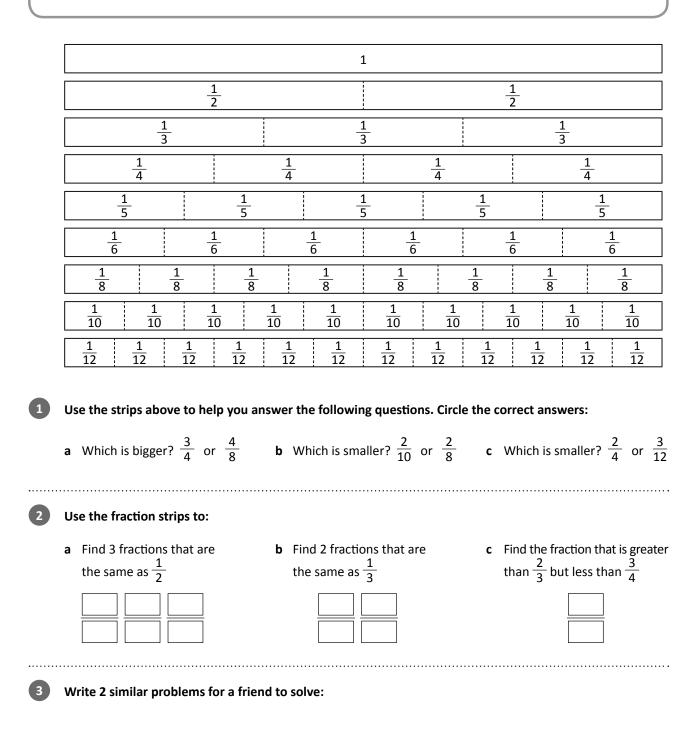
Find the fractional amounts. Use the space below to work out the different steps:





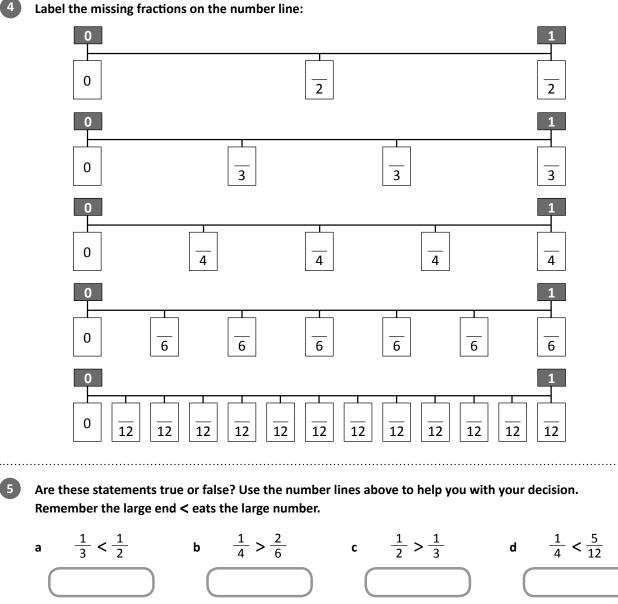
#### Fractions – comparing and ordering fractions

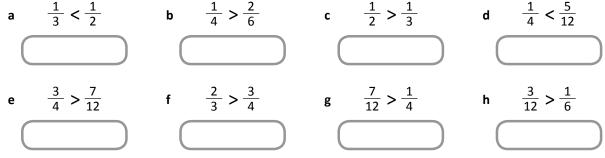
We can use number lines or fraction strips to help us compare and order fractions.



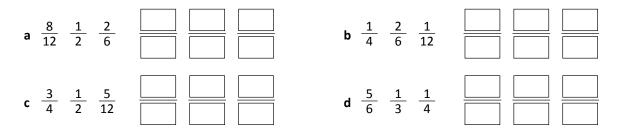


#### Fractions – comparing and ordering fractions





Use the number lines above to help you put these fractions in order from smallest to largest:





#### **Fractions, Decimals and Percentages**

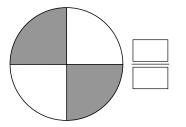
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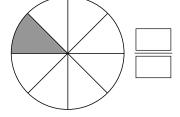
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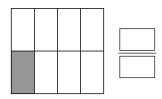
## Find the fraction

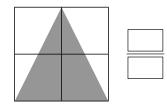


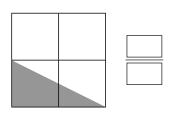
Your job is to work out what fraction of each shape is shaded. Some of them are simple to work out, others will take a little more thinking.

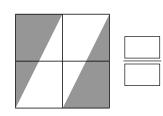


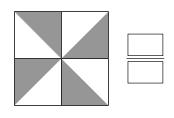


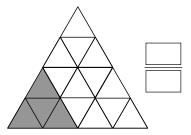


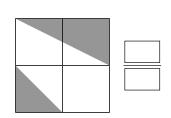






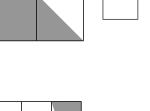




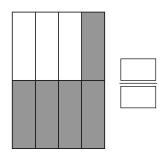




Hmm ... what will help me work these out? I could flip the shaded parts around in my head or maybe I could cut the shapes out and re-order them.









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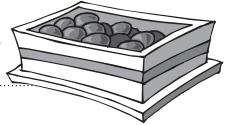
7

#### Mmmm, chocolate ...

apply



In this activity you will use your knowledge of fractions to share chocolates amongst a family.





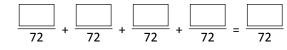
Mum gave you and your (imaginary) brothers and sisters a box of chocolates to share (also imaginary, unfortunately). She has decided to share them out based on how well you all cleaned your rooms. There are 72 chocolates in the box. Follow the directions to find how many you each receive:

- **a** Your sister Sarah can have  $\frac{1}{4}$  of the chocolates. How many chocolates is this?
- b Your sister Claire wished she had known this condition when she cleaned up her room. She can only have  $\frac{1}{12}$  of the chocolates. How many is this?
- **c** Your brother Angus did a stellar job on his room and is entitled to  $\frac{2}{6}$  of the chocolates. How many is this?
- **d** You get the rest! How many do you get?
- e What is your share expressed as a fraction?



Write an addition sentence to show how the chocolates were shared.

Now write a fraction addition sentence to show how they were shared.





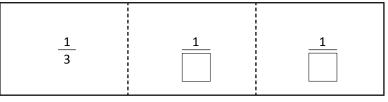
#### **Fractions, Decimals and Percentages**

### Types of fractions – equivalent fractions

Different fractions can have the same amount. They are equivalent. This pizza has been cut into 2 parts.  $\frac{1}{2}$  has been eaten. This pizza has been  $\frac{2}{4}$  has been eaten.

#### Do this folding paper activity to help you understand how equivalent fractions work:

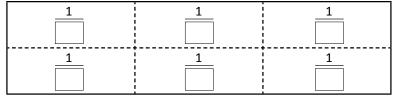
**a** You'll need a separate rectangular piece of paper similar to the one below. Fold it into 3 equal parts and then unfold it. Label each section with its fraction here:



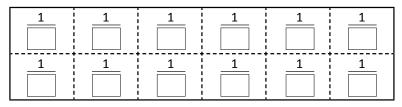
Remember the bottom number tells us how many parts there are in the whole.

.....

**b** Refold your paper into thirds and fold the thirds into halves. Unfold the paper. What fraction does each of the new sections represent?
 Label them here:



**c** Fold the paper back again and fold it in half once more. Unfold it and label the fractions here:



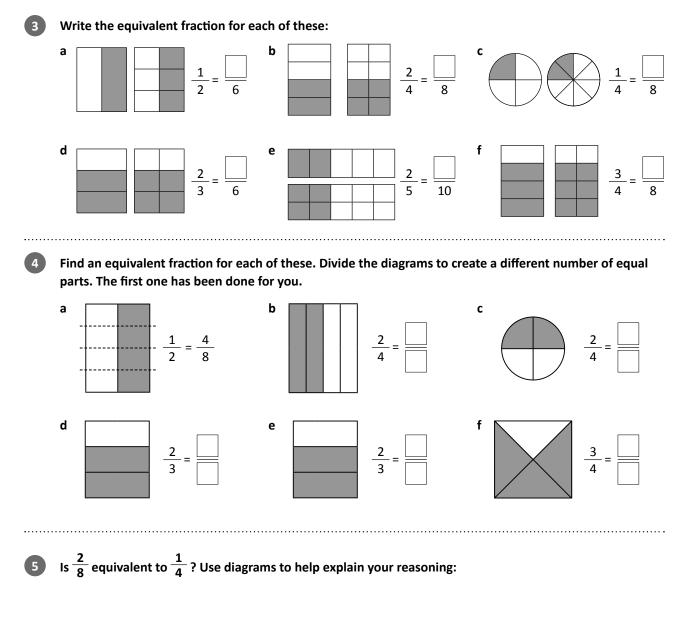
Use the diagrams in Question 1 to help you answer the following questions:

- **a** What fractions can you find that are equivalent to  $\frac{1}{3}$ ?
- **b** What fractions can you find that are equivalent to  $\frac{8}{12}$ ?
- **c** What other fractions can you think of that might be equivalent to  $\frac{6}{12}$ ?



9

## Types of fractions – equivalent fractions



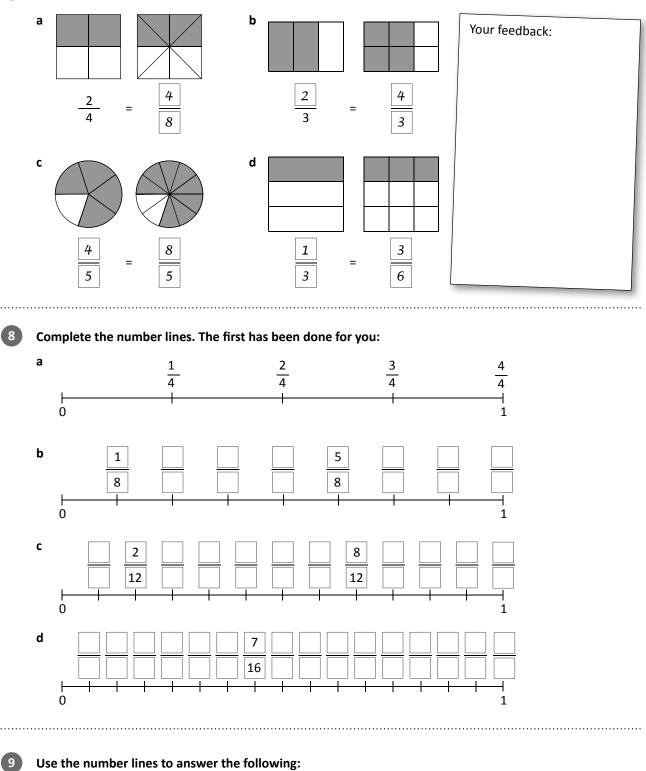
6 Is  $\frac{2}{3}$  equivalent to  $\frac{5}{6}$ ? Use diagrams to help explain your reasoning:



## Types of fractions – equivalent fractions



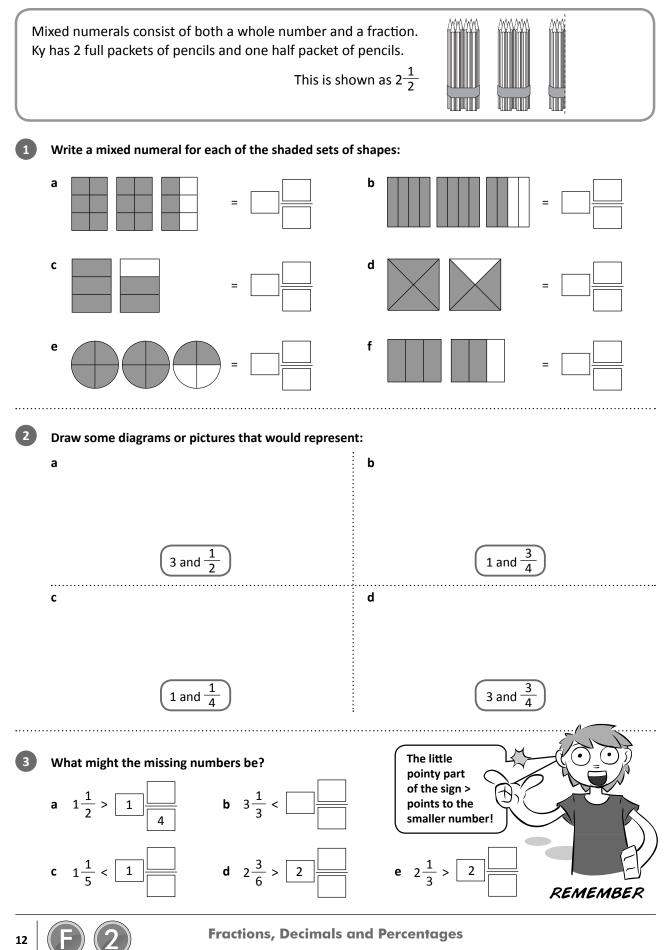
This section has been completed by our work experience boy. How did he go? Give him some feedback:



- **a** How many equivalent fractions can you find for  $\frac{1}{4}$ ?
- **b** Did you find a pattern? Can you continue it?



### Types of fractions – mixed numerals and improper fractions



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## Types of fractions – mixed numerals and improper fractions

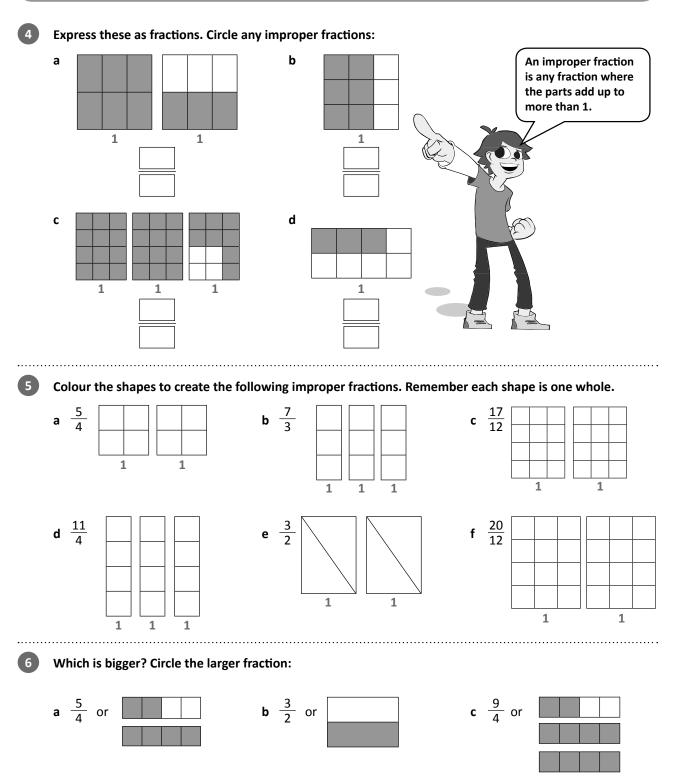
Mixed numerals can also be written as improper fractions. Look again at Ky's full packets and one half packet of pencils. This is five halves.

13

SERIES

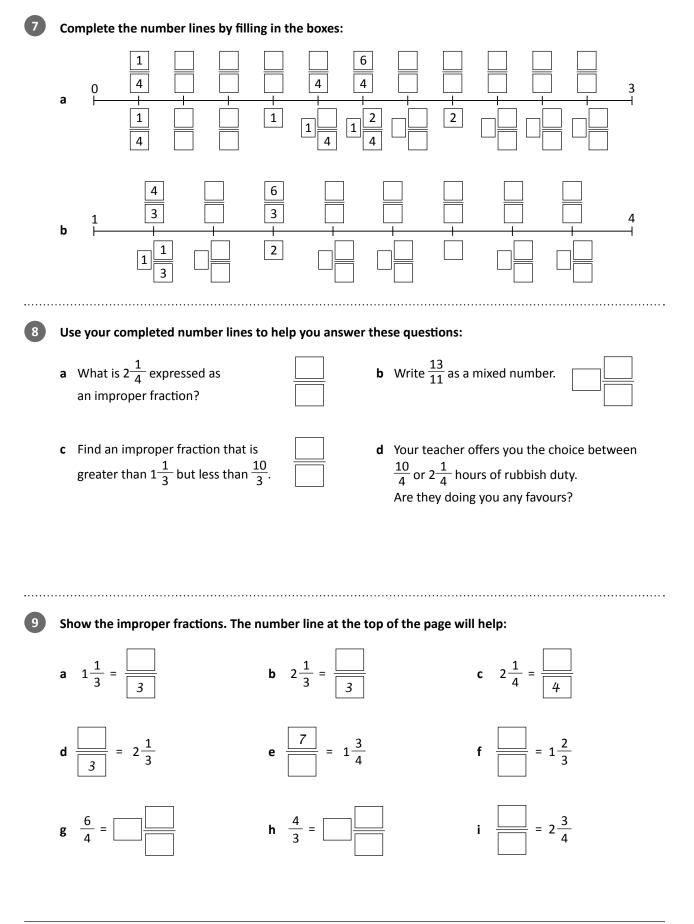
TOPIC

Written as an improper fraction, this is  $\frac{5}{2}$ .



Fractions, Decimals and Percentages

### Types of fractions – mixed numerals and improper fractions





Fractions, Decimals and Percentages

## Equivalent fraction snap

## apply



What to do Play this game with a friend. You'll need two sets of these cards. Make 2 copies of this page, cut out the cards and combine the two sets into one pile.



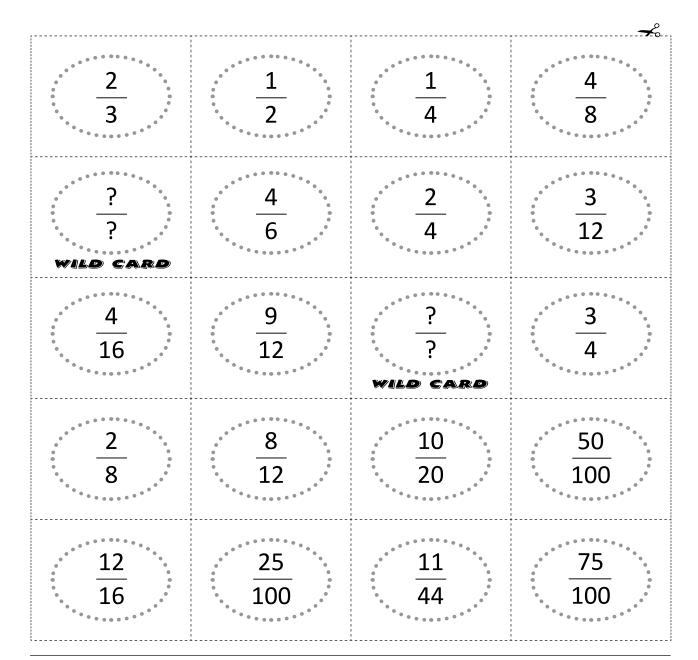
15

SERIES

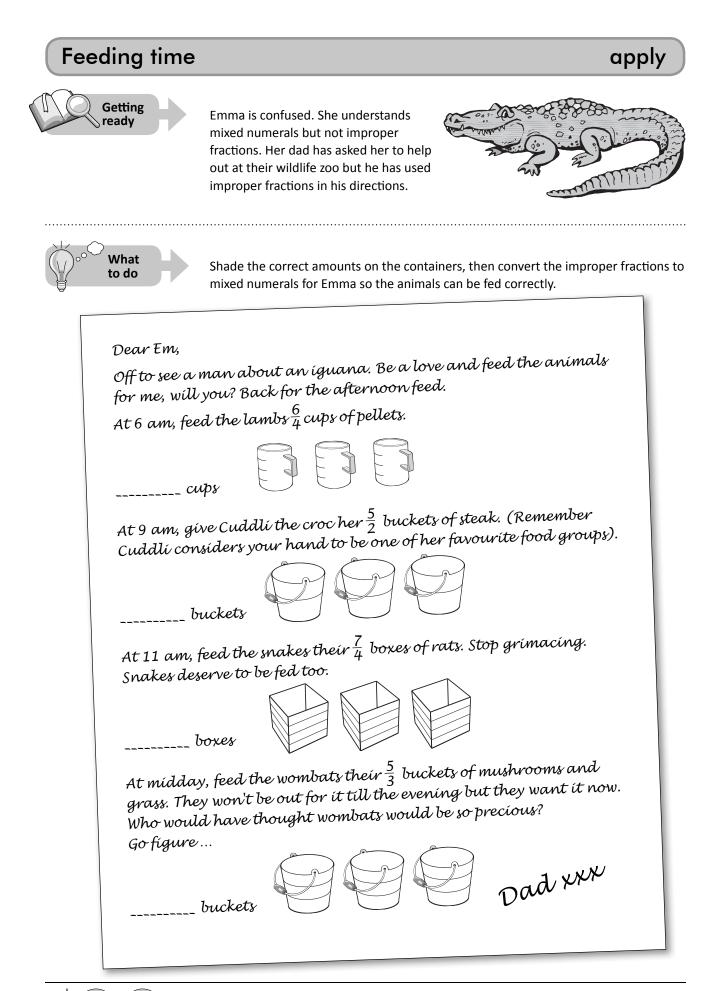
TOPIC

Player 1 deals the cards face down between the two players. Player 2 starts the game by placing a card in the centre. Players take turns in turning over the top card on their pile and placing it in the centre pile. Call, "Snap!" and take the centre pile if the card is identical to or an equivalent fraction to the card already face up.

The four wild cards can be used to make a Snap! When playing a wild card, you must name a correct equivalent fraction. The person with all the cards at the end is the winner.



Fractions, Decimals and Percentages





16

#### Fractions, Decimals and Percentages

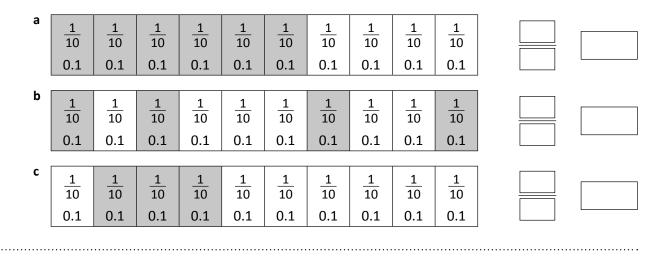
#### Fractions, decimals and percentages – tenths

Decimal fractions also express parts of a whole. This strip has been divided into 10 equal parts. Three out of ten or  $\frac{3}{10}$  is shaded.

$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	<u>1</u> 10	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$
0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1

We can also express this as 0.3. There are no wholes and 3 tenths.

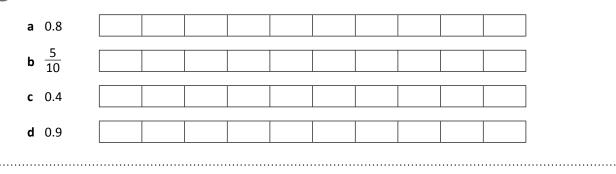
Write the shaded common fraction and its equivalent decimal fraction:



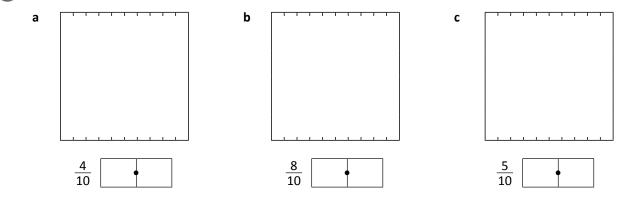
Shade the fraction strips to match the common fraction or decimal fraction:

2

3



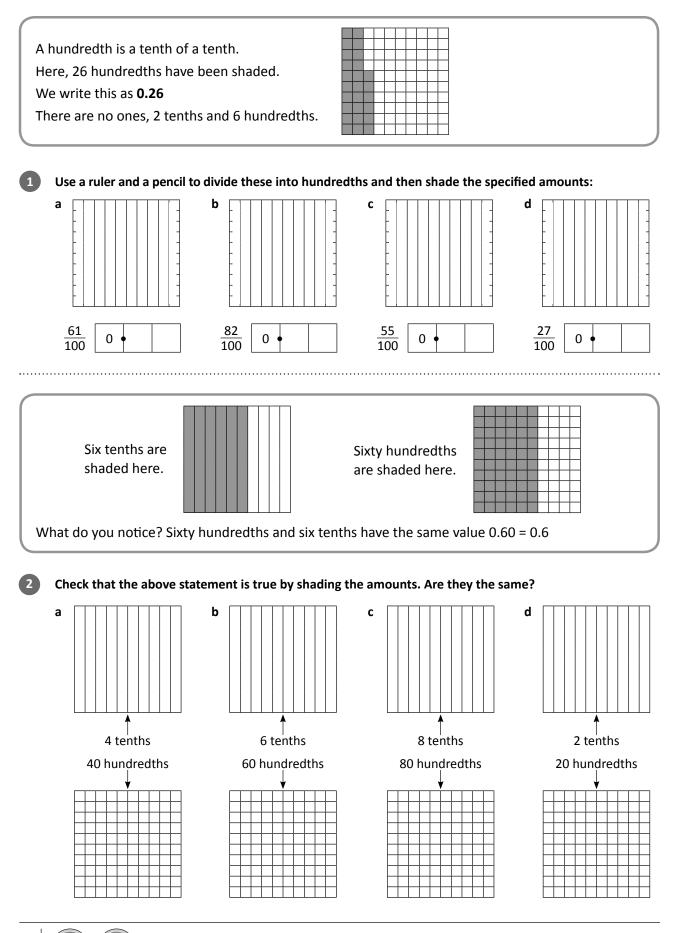
Use a ruler and a pencil to divide the wholes into tenths. Shade the given amounts and express as decimals:



TOPIC

SERIES

#### Fractions, decimals and percentages – tenths and hundredths



**Fractions, Decimals and Percentages** 

18

SERIES

TOPIC

#### Fractions, decimals and percentages – tenths and hundredths

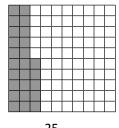
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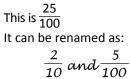
а

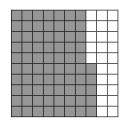
Complete these statements. The first one has been done for you.

b

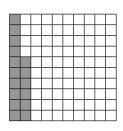
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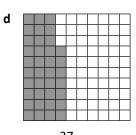


This is  $\frac{75}{100}$ It can be renamed as:



С

This is  $\frac{16}{100}$ It can be renamed as:

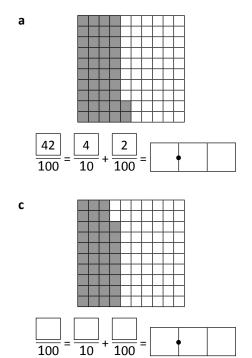


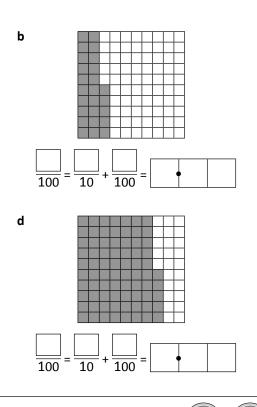
This is  $\frac{37}{100}$ It can be renamed as:

It can be renamed as:

This represents 2 wholes and  $\frac{75}{100}$ 

Complete the missing information:





Fractions, Decimals and Percentages

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TOPIC

## Fractions, decimals and percentages – decimal place value

A hundredth is a tenth of a tenth.

Ones		Tenths	Hundredths				
2	•	2	5				

This number has 2 ones, 2 tenths and 5 hundredths.

#### Write these numbers in the place value chart:

	Thousands	Hundreds	Tens	Ones	Tenths	Hundredths
a 5 tens, 3 ones and 8 tenths					•	
<b>b</b> 7 hundreds, 8 tens, 4 ones, 2 tenths and 3 hundredths				•	•	
c 9 tens and 8 tenths				•	•	
<b>d</b> 6 hundreds, 8 tenths and 4 hundredths			0	0 •	•	
e 4 ones, 9 tenths and 8 hundredths					•	
f 3 ones, 4 tenths and 2 hundredths				•	•	
g 2 tens, 3 ones and 4 hundredths					0	

Answer true or false to the following questions. Score 0.5 points for each correct answer.

- **a** The value of 4 in 56.48 is 4 hundredths.
- **b** The value of 3 in 38.65 is 3 tens.
- **c** The value of 7 in 0.75 is 7 hundredths.
- **d** Thomas thought of a decimal number between 5.61 and 5.91. The number could have been 5.64.
- e 97.3 is 9 tens, 7 ones and 3 hundredths.

T or F	Score
Total	



20

2

#### Fractions, decimals and percentages – decimal place value

When comparing and ordering decimals, the place value of a digit is crucial. The further the digit is to the left, the greater its value.

Even though one hundredth sounds big, it is actually very small. Remember, one hundredth is just a single piece of a whole divided into a hundred parts. One tenth is actually ten times bigger than one hundredth.

3	Which is bigger?	Circle the correct a	nswer	:							
	<b>a</b> 0.7 or 0.07	7	<b>b</b> 0.	56 or	6 tenths		c 7	7.5 o	$r \frac{7}{10}$		
	<b>d</b> 15 or 0.15	5	e <u>1</u> 2	or C	).25		f 3	85 or	3.5		
4	Use < or > or	= to show the relat	ionshi	p betwe	en the two	numbers:					•••
	<b>a</b> 6.89	6.76	b	9.08	9.8		<b>c</b> 11	1.80		_ 11.8	
5	This chart shows	the vital statistics o	of som	e Rooste Height	ers Footbal	l Club players Weight			đ	00	
		Lanky		2.06 m		79.05 kg	٦.		1	-1	
		Crusher		1.96 m		110.65 kg		4	-		
		Crumber		1.73 m		79.93 kg					
		Cazaly		1.84 m		88.91 kg		G	000-		١
		Stomper		1.81 m		99.55 kg		G			)
		Whale		2.01 m		118.23 kg			۹L		
		Twinkle Toes				65.78 kg					
	<b>a</b> Who is tallest	? Who is shortest?					_		A		

**b** Put these players in order of lightest to heaviest: Crumber, Stomper, Cazaly:

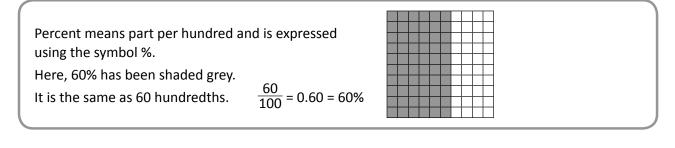
c Which 2 players would you have playing in the ruck? (Rucks have to be tall.)

d Who would you least like to have tackle you? Why?

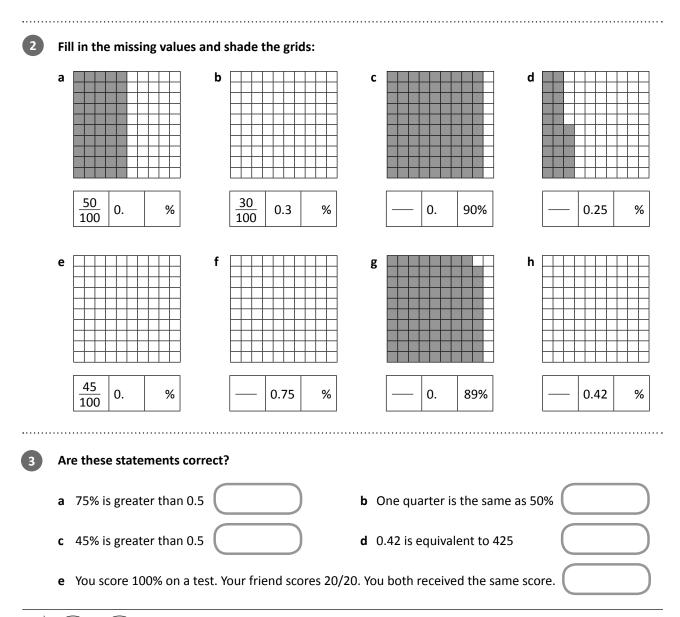
**e** Twinkle Toes twirled out of the club before his height was measured. We know he is taller than Crumber and shorter than Cazaly. What could his height be? Add it to the table.



#### Fractions, decimals and percentages – percentages



Think of at least five times you see the % sign or use percentages:

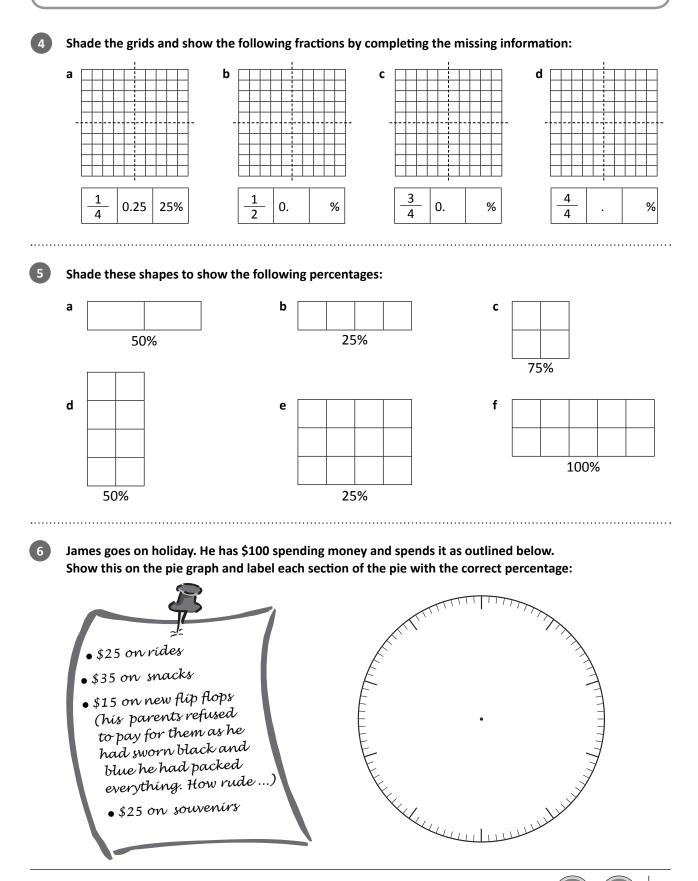




#### **Fractions, Decimals and Percentages**

#### Fractions, decimals and percentages – percentages

It is useful to know some common percentages such as 25%, 50% or 75%.



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23

TOPIC

SERIES

### Match 'n' snap

## apply



This is a game for 2 or more players. You will race against each other to come up with equivalent fractions, decimals or percentages to match those on cards. You'll need one copy of this page and one copy of page 25 between you.





Cut out the playing cards, mix them up and put them face down in a pile.

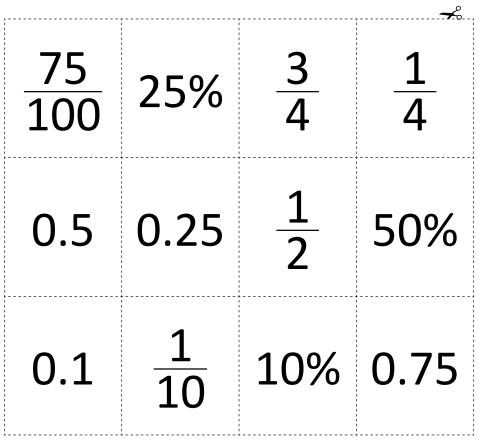
Cut out the blank cards on page 25 and divide them between the two of you. Make sure you both have a pencil each.

Turn over the first playing card. Both players write an equivalent fraction, decimal or percentage to match it on one of the blank cards and cover the playing card as quickly as possible.

For example, the playing card may say 50% – you could write  $\frac{1}{2}$  or  $\frac{5}{10}$  or  $\frac{50}{100}$ .

The first person to cover the card with a correct match wins and takes the pair. The player at the end of the game with the most cards is the winner.

#### **Playing Cards**





## Match 'n' snap

#### **Blank Cards**

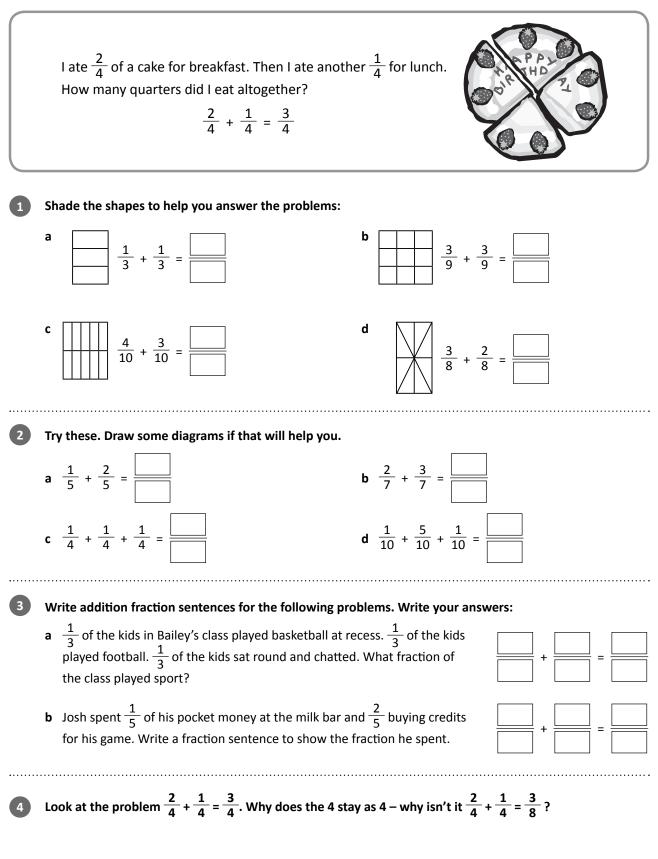
Biank Cards											
			, , , , , ,								
			, , , , , ,								
			, , , , ,								



apply

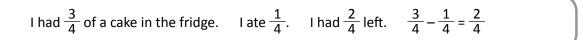


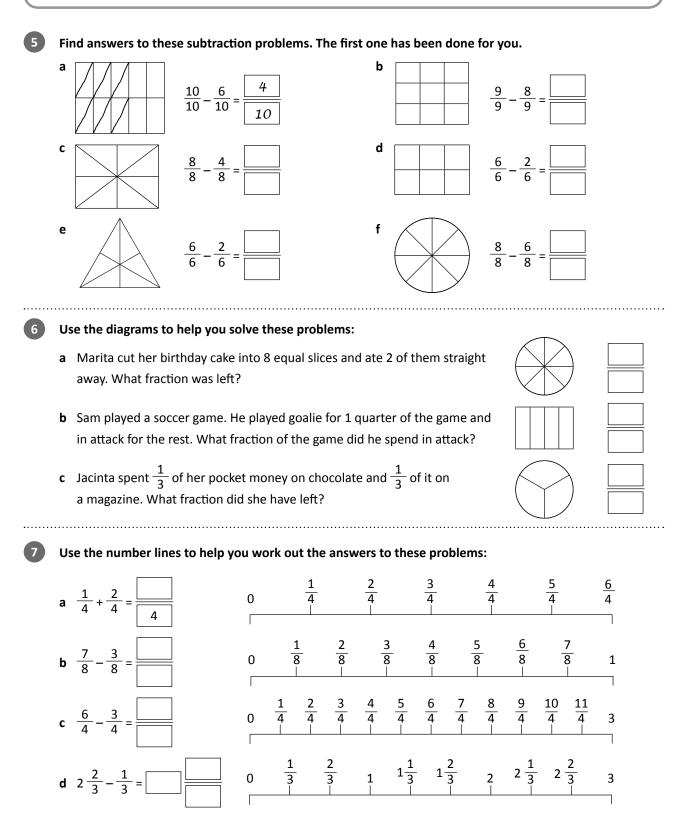
## Calculating – adding and subtracting fractions with like denominators





## Calculating – adding and subtracting fractions with like denominators

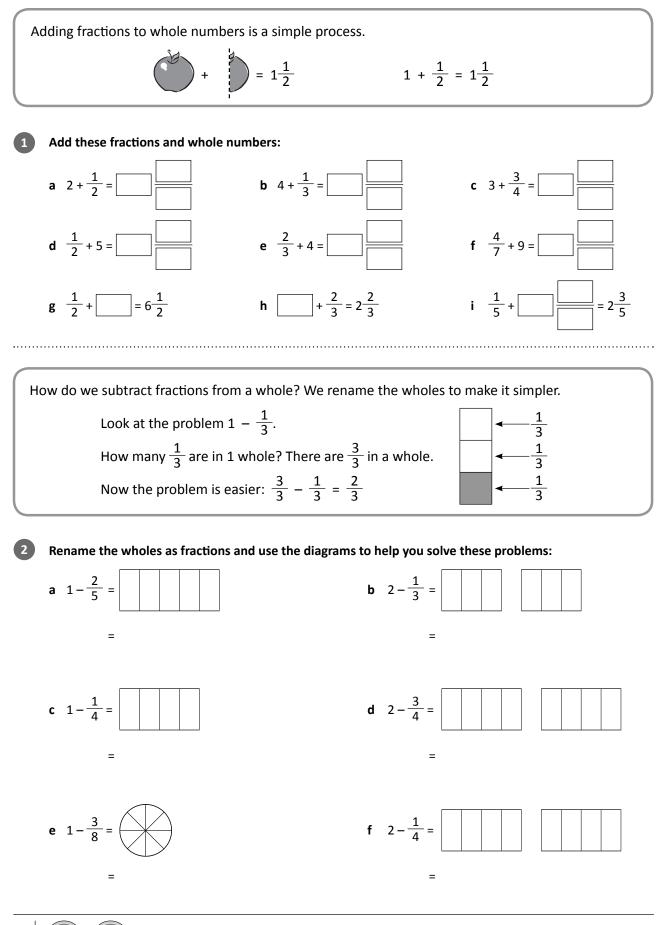






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#### Calculating – adding and subtracting fractions to and from a whole





28

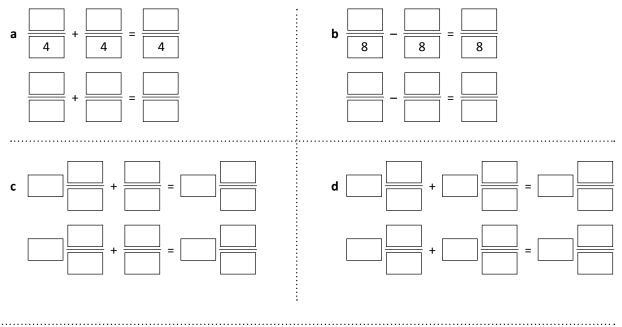
Fractions, Decimals and Percentages

## Calculating – adding and subtracting fractions

1

2

#### What could the missing numbers be? Create two different options for each:



Solve these problems. Draw diagrams if they help:

**a** You have  $3\frac{1}{4}$  packets of cookies. One friend eats  $\frac{1}{4}$  packet, another eats  $\frac{2}{4}$  and another eats  $\frac{1}{4}$ . What fraction do you have left?



**b** What fractions do you know that have a difference of  $\frac{1}{4}$ ?



Now I could also use





## Calculating – adding decimal fractions

(	
How do we add decimal fractions using a written strategy?	
We arrange the numbers so the place values line up and then we start with the smallest value.	
We first add the tenths. 6 tenths and 7 tenths is 13 tenths.	<sup>1</sup> 1 . 6
We rename this as 1 whole and 3 tenths.	+ 4.7
We write the 3 in the tenths column and move the 1 to the wholes column. Then we add the ones. 1 + 1 + 4 = 6	6.3

1 Knowing how to rename is a useful skill when adding decimal fractions. Practise your renaming skills here by colour coding the matching boxes:

			10	) tentl	ns					23	3 ter	nths	)		(	2 one	s and	l 3 te	nth	s		
		18	tenth		58 hun	dredths		4	14 hu 7 c	ndreo ones a			nths	) (	14	hund	( redth	76 t	ent	hs	)	
		11	tenth	and 4	hundr	edths	)			(		1 o	ne	$\supset$				one	and	d 8 te	entł	ns
	4	ones	, 1 ter	nth an	d 4 hu	ndredth	s		Œ	5 tent	hs a	nd 8	3 hur	ndred	ths	)						
2	Ado	d thes	e dec	imal f	ractior	IS:															•••••	
	а			. 6				b				•				С			5			
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•••••	•••••					- 		•						-								
3	Nov	w try	these	. Start	with t	he hun	dredt	:hs a	nd re	mem	ber	to re	enan	ne if r	necco	essary	<i>י</i> :					
	а		3.	4	6		b		4	. 7	7	2			С			7	•	3	6	I.
	_	+	5.	2	3		_	+	3	. 2	1	9	-		_	+		5	•	6	5	
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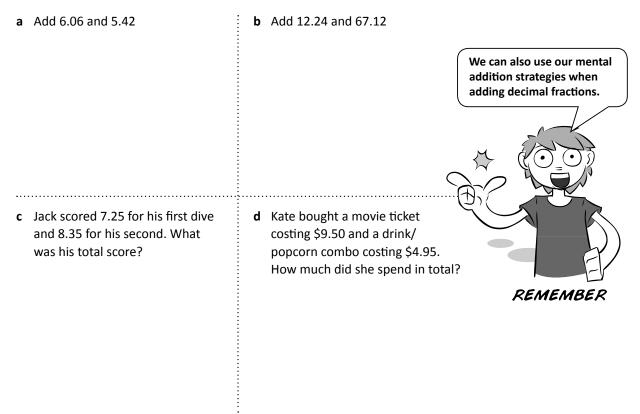
#### **Fractions, Decimals and Percentages**

## Calculating – adding decimal fractions

4

5

Use a mental or written strategy of your choice to solve these problems:



.....

#### This is a sample of the menu at Laura's Lunches.

- **a** Brad orders a souvlaki, a bucket of hot chips and an orange juice. How much will this cost him?
- **b** Angelina goes wild and orders a sushi roll, a bottle of water and a piece of fruit. What will this cost her?
- **c** Choose your own lunch. Itemise your list and calculate the total value of your order.

#### Laura's Lunches Salad sandwich 4.25 Sushi rolls 2.20 Hot chips 1.95 Souvlaki 7.35 Fruit .60 Stirfry noodles 4.95 Slurpee 1.55 Orange juice 1.95 Bottle of water 2.15 Choc or banana muffin 1.85

F 4 31

### Calculating – subtracting decimal fractions

How do we subtract decimal fractions using a written strategy?	
We arrange the numbers so the place values line up and then we start with the smallest value.	F 1
We first subtract the tenths. We have 2 tenths, can we subtract 5 tenths from this?	? <sup>5</sup> 6 . <sup>1</sup> 2
No, so we rename a one as 10 tenths. Now we have 12 tenths. 12 tenths subtract	- 4.5
5 tenths is 7 tenths.	1.7
We have 5 ones, can we subtract 4 ones? Yes, the answer is 1 whole.	

Solve these subtraction problems: 8.3 4.7 5.4 b а С 2.2 3.4 3.5 8.6 d 2.3 f 9.4 1 е 1 5.2 1.2 3.7 1 ..... Now try these. Start with the hundredths and remember to rename if neccessary: 2 8.4 b 4.7 2 8.4 4 С 6 а 3.2 4 2.2 9 1.6 3

Sometimes we have to work with numbers that have a different amount of digits such as **8.4 – 5.35** When this happens, we rename. 4 tenths becomes 40 hundredths: **8.40 – 5.35** 

Rename these problems and solve:

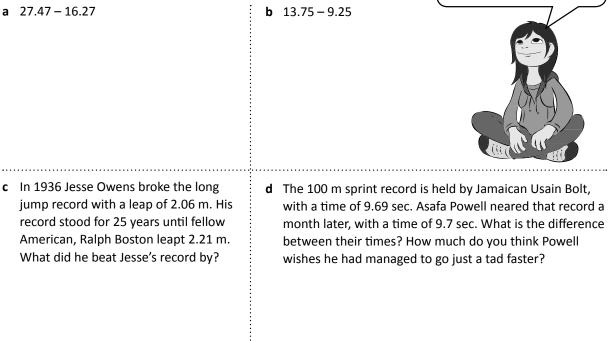
а		9.	5		b		6	1	7	С		9	3	
	-	2.	2	4		-	2	3			-	4	7	2



### Calculating – subtracting decimal fractions



- Use a mental or written strategy of your choice to solve these problems:
- We can also use our mental strategies when subtracting decimal fractions.





Belle's basketball team measured their heights and entered them on the chart. What is the difference in heights between:

- a Suzy and Lucy?
- **b** Ti and Natasha?
- c Nina and Belle?

d The tallest and shortest girl?

1.43 m Ti 1.37 m Grace 1.47 m Marietta 1.42 m Madison 1.54 m Lucy 1.58 m Belle 1.61 m Natasha 1.53 m Donna 1.34 m Nina 1.53 m

**Belle's Beauties** 

Suzy



#### You cut, I choose



You and your friend have been asked to attend a tea party. Your host, Mr Hatter, has made a chocolate clock cake for the festivities, but clearly he got a little mixed up with his numbers. It must have been all those pre-party nerves, or quite possibly the punch.





Anyway, he has asked you to cut the cake into 3 pieces so that each of you gets a piece with the numbers adding to the same total. How do you do it? Show your cuts on the clock cake below.

Each piece totals \_\_\_\_\_

.....

Work out what fraction of the cake each of you receive. I should warn you, Mr Hatter wants the biggest piece.

